Formalising social representation to explain psychiatric symptoms

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Abstract

Recent work in social cognition has moved beyond a focus on how people process social reward to examine how healthy people represent other agents and how this is altered in psychiatric disorder. However, formal modelling of social representation has not kept pace with these changes, impeding our understanding of how core aspects of social cognition function, and fail, in psychopathology. We suggest that belief-based computational models provide a basis for an integrated sociocognitive approach to psychiatry with the potential to address important but unexamined pathologies of social representation such as maladaptive schemas and illusory social agents.

Highlights

- Bayesian-belief models formalise rich state-spaces and use full posterior
 probability distributions that can characterise and extend sociocognitive theories;
 they also offer an opportunity to test psychiatric theories that implicate changes in
 the structural representations of self and others.
- Tasks that involve a range of joint outcomes for the participant and their partner(s) interrogate critical aspects of complex social processing, and better reflect how we come to know other minds.
- Computational models of social representations provide a test-bed to examine
 how uncertainty, social decision making, and learning processes contribute to
 core psychiatric phenomenology, such as social schemas and the production of
 illusory social agents in psychosis.

Formalising social representation

The field of cognitive neuroscience has taken important steps toward uncovering the mechanisms by which we build representations of our environment. Integrated experimental and theoretical work suggests we encode, organise, recall, and generalise knowledge within cognitive structures to allow for flexible behaviour [1-4]. There is now ample evidence that social information is structured in a similar way [5]; relationship structures, mental states, traits of individuals and social environments can be mapped as conceptual representations that are recoverable from experimental investigations [6], observational studies [7], and neural activation [8,9]. One notable feature of social environments is that they are highly interactive – we react, cooperate, compete, and conflict with other agents who have their own beliefs, desires, and traits. Therefore, humans need methods for dynamically modelling other agents [10], and by extension, theorists working in this domain require computational models that can adequately represent this state space. However, while many elements involved in goal-directed non-social information processing have been captured through computational models that centre on model-based learning and prospective reasoning [11-12], the use of formal computational models to conceptualise social representation are relatively newer [13-16].

Computational models allow an integration of biological and psychological determinants of decision making to provide refined explanations of mental disorder that cut across multiple levels of explanation [17]. Indeed, changes in how we encode and predict basic value information in the environment have been used to explain biases related to delusion formation [18-19] and hallucinations [20-21] where overweighted and rigid prior beliefs coupled with sensory uncertainty generate aberrant perceptions and false beliefs. Similarly, reinforcement learning (RL) models have been useful when characterising major depressive disorder [22] and anxiety [23]; artificial neural networks have been proposed as models of aberrant perception [24]; attractor state models have been used to explain probabilistic reasoning in delusions [25]. Psychiatric disorders frequently, and sometimes fundamentally, involve alterations to social perception and behaviour [26-27], meaning computational models of social interaction in psychiatric disorder, although still nascent, are an exciting development in cognitive science [28-30].

In this review, we provide a framework for examining how belief-based generative models can be used to specify and test hypotheses about how people (which we refer to as 'selves' or 'self') infer the presence of, and represent, other agents ('others' or 'other') during social decision-making. We first consider normal function; and then look at how these models have been, or could be, applied to understand psychiatric disorder. Our research and this review focus on approximate **Bayesian models** that consider the uncertainties that individuals have about their beliefs, and how these uncertainties affect both inference and learning. Bayesian models offer a versatile and clear framework for representing individual and interactive task spaces [16,31-32]. Since reasoning about others involves considering a self's own model of the other in a specific context, it would be incomplete to use generic (e.g., neural network) models to explain interactive

learning. Even if generic models are used in a model-free manner to distil the interaction, model-based methods would still provide essential understanding.

We collectively refer to formal theoretical models which make claims about the probabilistic structure of self and other mental states as computational social representation models. We develop our ideas from foundational work which outlines the importance of rich computational techniques to explain general economic [13] and social psychological phenomena [15,17,33] and the role of social representation in social cognition and psychiatric disorder [34-38].

Social representations and psychiatric disorder

Inherent aspects of social interaction (uncertainty, contextual reward, and social dependencies) lend themselves to structured, probabilistic models, with Bayesian formulations modelling how uncertainty about others' intentions can be integrated into social decision-making. 'Structured probabilistic model' refers to a generative hypothesis that links prior probability distributions, e.g. the probability that a self values equality or the self's assumptions about an other's preferences for equality, to value functions, e.g. the probability that the self will be prosocial in this moment or an other will act prosocially. Variance within each distribution allows for the quantification of uncertainty over the experimenter's parameter approximation of a self. It also allows experimenters to model a self's own epistemic uncertainty of their characterization of themselves and their environment (Figure 1; reviewed in [14]; also see [39-40]). It is often the case that these two forms of uncertainty may be hard to distinguish using practical experimental procedures, and so robust fitting procedures should be used (see Outstanding Questions). These dimensions provide multiple abstract representations of value components of self and others (e.g., uncertainty, valence) that reward-learning models of decision-making exploit to generate appropriate value signals [41]. Iterative game theoretic tasks (see Box 1; reviewed in [33]) have offered particularly fruitful paradigms for modelling social interaction where a self's internal representations of the other agent(s) are required for drawing task-relevant inferences.

Here we review formal theories that are intended to model generative processes in social cognition. We focus on models which characterise the self and other(s) using rich **state spaces** and consider their use for probing psychiatric disorder (for a summary, see Table 1), drawing from and extending previous work [14,33]. We adopt model classes which embody different temporal, recursive, and causal structural features (for a visual summary see Figure 2, Key Figure): shallow Depth-of-Mentalisation (DoM; including a self's beliefs, and a self's beliefs about the other given past actions), hierarchical DoM (self-beliefs about how the self's actions will influence the other's actions at different levels of recursion), and Group Mentalisation (how the self may hold beliefs about multiple others). We note here that while RL formulations of social interaction have been developed, may fit within our taxonomy, and make important contributions [42-46], these are not the focus of our review. Nevertheless, we hope our taxonomy provides a useful framing for wider work in this area.

Shallow Depth-of-Mentalisation

Shallow Depth-of-Mentalisation (sDoM) models allow experimenters to formalise hypotheses about the beliefs of the self (their motivations, mood, and intentions), and the beliefs the self holds about an interaction other's internal state, conditioned on their past behaviour ([14]; Figure 2A). sDoM are shallow in the sense of not including the sort of deeper social recursion and cognitive hierarchy that we consider later. These models may be important in cases where hierarchical social planning is restricted [47] or when selves are simply observing others, rather than interacting with them (in a gametheoretic sense).

One role of sDoM models is to probe inferences about the internal representations of external agents from observation alone. For example, building on descriptive accounts of rational action planning [48], experimenters tested how selves predict the action path of an other's movements around a 2D grid (a 'maze-world') given the cost of action and action variability [49-51]. Likewise, prior work [52] has used a gambling task that required selves to infer emotions of an other based on the integration of facial cues, utterances, and financial results. sDoM models have also been used to investigate the approval rate of individuals within a group following feedback, and the subsequent impact on self-esteem [53]. Given the basic disruptions in mental state inferences as observed in schizophrenia [54], these models provide a formal platform to assess when greater consistency in an other's actions ceases to be an inferred reliable predictor of their hidden motives, and the conditions under which models that explain the link between inference and action may begin to fail.

Socially-regarding paradigms (Box 1) take the step of considering interaction between self and others. These permit investigation of the effect of joint outcomes on action selection and beliefs, and formally address how social context influences cognitive dynamics, such as learning and uncertainty. One example is the use of a repeated Trust Game and a slot machine paradigm to study generalised anxiety disorder [55]. In the repeated Trust Game, one participant is an investor who may choose to send a proportion of an endowment to another participant, who acts as the trustee. The experimenter scales the investment by a multiplicative factor (e.g. three); the trustee can then choose how much to send back to the investor. The game is played over multiple rounds, with the investor and trustee adopting the same roles each time. Within this task it has been reported [55] that selves more heavily weighted social losses compared to non-social losses, and positive first impressions lasted throughout social, but not non-social contexts when updating beliefs about the trustworthiness of the other. Selves who scored above the clinical cut-off on a generalised anxiety disorder scale showed a selective reduction in learning about exploitative partners and negative events, and a failure to enhance learning as social uncertainty increased. This result goes against the conventional Bayesian expectation that learning should rise because of epistemic uncertainty (if a model is not yet reliable, more sampling is needed), suggesting a general insensitivity to uncertainty. Results also contrast with RL models [23] which suggest that in non-social contexts, negative (rather than positive) outcomes are overvalued in those with high anxiety. Nevertheless, specific task demands may

preclude comparison between parameter estimates derived from either study, and care must be taken when generalising parameter estimates into new contexts.

Social-regarding paradigms have also been used to understand better the coupling of policy uncertainty with priors and **likelihoods** over mental state attributions during interactions in an iterative Dictator Game [56-58]. These models provide formalisations that encompass earlier ideas about the predictive mind in social cognition [35], e.g. the flexibility over attributions (trait), probabilities over the current intentional motives of the other (state), and subsequent attributional change (action). As a result, these models allow core computational theory to be extended to characterise an environment that allows for joint social dependencies, and to probe clinically-relevant phenomena (e.g. multiple mental state attributions) while retaining core computational facets (learning; uncertainty).

Multi-phase task structures allow simultaneous approximation of multiple representations and can assess how the self's beliefs change following social observation, or how the self suppresses updating of irrelevant representations to use context-appropriate beliefs (Figure 2B). To note, these designs probe the neutrality of self after social observation; being exposed to others may alter self-preferences [59] or effect inferences about the self [60]. Inter-temporal discounting tasks [61-63] estimate whether a self prefers a smaller monetary reward now or a larger one at a later time point (phase 1), how a self learns about an interaction other's preferences (phase 2), and whether exposure to an interaction other changes the self's preferences (phase 3). By estimating belief distributions about each agent [60] experimenters can approximate the causal influence of exposure to an other on the beliefs of the self (e.g. being exposed to a patient other can inspire greater patience in the self) and the way this depends on the self's initial uncertainty about themselves (and, putatively, the assumed similarity between the two).

Multi-phase designs have been extended to social regarding contexts, testing how self social-value preferences integrate into beliefs about the social-value orientation of an other, and how paranoia may distort this process. This extends prior assessments of how social influence may govern a self's SVO [64]. Using models that estimate the preference for relative and absolute joint payoffs (Figure 1; [65]), experimenters can estimate how uncertainties and social orientation of self-preferences may disrupt the process of learning about the social-values of an other along multiple, contextually relevant dimensions (i.e. relative versus absolute payoff preferences). These multiphase configurations allow testing of key psychiatric phenomena, such as the misattunement hypothesis [66], with results suggesting that discrepancies in self-other representations may make individuals more prone to developing paranoid explanations of social events [65]. Extending prior imaging work using multiphase paradigms [61-63], it will be useful to probe whether computational biases as a function of paranoia are reflected in reduced functional modelling of others, whether therapeutic outcomes may be marked by increased functional modelling of others, and importantly, whether this is reflected in positive outcomes.

Hierarchical Depth-of-Mentalisation

Hierarchical Depth-of-Mentalisation (hDoM) models capture the recursive inference of value-functions between two players in strategic planning. hDoM are used to formalise how agents model first, second, or k^{th} -order nested beliefs (e.g. the self's model of the other's model of the self's model of the other etc; Figure 2C) [67-69]. This can then branch-off over the orthogonal dimension of multiple steps of forward planning, when self and other interact over several rounds [47, 70-73]. Such models therefore formalise the processes underlying social dependencies between self and other [14].

For example, in the Trust Game, one major factor governing the interaction is inequality aversion. If the trustee can persuade the investor that she is inequality averse, then the investor has a reason to trust that it is safe to invest. Recursive reasoning about inequity aversion in the Trust Task proceeds as follows: a level 0 investor would consider their actions in light of their beliefs about the trustee (based on the trustee's history of decisions; e.g.[55]); a level 1 Investor would also consider the beliefs the trustee holds about the investor, and therefore how the investor's own actions may influence the trustee's subsequent actions in this and future rounds; a level 2 investor considers their actions in light of a model that encompasses the belief in the trustee's beliefs about the investor's beliefs, and so on.

Recursive modelling has been employed in a ten-round version of the repeated Trust Game [74-75]. This extends local behavioural assessments of coaxing by an other [76]. Experimenters tested hypotheses about the level of such modelling and the degree of forward planning in which trustees or investors indulge as they make their choices. It has been found, for instance, that people with borderline personality disorder (BPD), when acting as trustees, have shallower recursive depth than healthy volunteers [74]. Later versions have characterised additional factors, including a form of risk aversion of the investor, operationalised as their reluctance to invest because of the danger of a poor return by the trustee; and (state) irritation, which accumulates according to (trait) irritability in the light of unsatisfactory behaviour of the partner and leads to a breakdown of recursive reasoning, forward planning and cooperation [77-78]. People with BPD are more irritable as trustees.

The Stag Hunt Game is a microeconomic game of cooperation: two players (as hunters) can capture a stag if they both opt to do so and will both be rewarded with many points. However, either or both players could instead opt individually to capture a rabbit which is worth fewer points. If one opts for the stag, the other for the rabbit, then only the latter gets any points. The stag hunt game has been modelled similarly to the Trust Game to approximate the forward-planning of selves [79], and how forward-planning may be implemented in the brain [80]. Importantly, this model has been used to test those with autism spectrum disorder (ASD). Experimenters found that while controls were best fit by a recursive model that considered the strategy of the other, selves with ASD were best fit by a fixed model which contained significantly less recursive depth and were less flexible (were more tied to past strategies), despite being no different to controls in their cooperation rate overall [81]. This finding converges with later work using a hDoM

model [82] during a 'hide and seek' game [83]; those with ASD were less flexible in their strategy when compared to neurotypicals and displayed shallower mentalisation, although this was only a disadvantage when paired with a social versus non-social other.

The convergence of shallower forward-planning during social paradigms in individuals diagnosed with either BPD or ASD is intriguing given their respective symptom profiles - ASD reflects an under-sensitivity to social cues whereas BPD reflects an oversensitivity. Here, computational modelling has the potential to disentangle how each may show similar behavioural phenotypes but with distinct underlying mechanisms. For example, the introduction of irritability [77-78] makes it possible to assess whether reduced forward planning performance in those diagnosed with BPD can be explained by exaggerated irritation rather than a deficit in forward-planning per se. Likewise, it may be that under different social contexts (e.g. cooperation versus competition), forward-planning becomes restricted or not used to inform decision making (e.g. [81]) and may highlight where ASD and BPD diverge. Notably, when prosocial behaviour is sufficiently predictive, selves may not need to develop sophisticated models of their others [79]; a form of equilibrium can be achieved through simple prosocial social-value biases, which may be less computationally costly [84]. Therefore, those with ASD may have difficulties forming complex, sophisticated models of others, rather than a deficit of basic associative processes. Indeed, there are normative contextual predictions about forward-planning that can be used to test divergence: higher levels of strategic planning are optimal under competitive conditions [70-71, 82] and lower levels of sophistication are optimal under cooperative conditions [93].

Group Mentalisation

Although most models aim to understand social interaction on a one-to-one level, understanding and strategising based on group characteristics, such as collective beliefs, actions and group identity, are also a key part of navigating the social world. Generative processes hypothesised to govern social categorisation have been formalised using non-social regarding preference tasks ([86]; Figure 2D). In one such example [87], the self is required to infer the group membership of others by observing their pattern of preferences that include socially benign characteristics (e.g. movie choices). In another, participants learn characteristics that more strongly determine action and judgement (e.g. political / moral beliefs) [88]. Models of social structure learning [87-90] explain the statistical process through which selves assign others to social clusters, and how the influence of group members may distort social categorisation e.g. similarity to a member of the group.

Social-regarding beliefs a self holds about a group have been modelled using the Public Goods Game (PGG), where selves secretly decide how much money to contribute to the group. The total amount is multiplied by a factor of *i* (between 1 and the total number of players) and is then distributed evenly among all players, including any who declined to contribute themselves. Modelling of the PGG has suggested selves statistically represent a group as a single entity [91]. This has been extended to use a

blend of individual utility and group utility functions, estimating the joint utility of a self's own investment into the group, and their belief that others in the group would free-ride [92]. Deeper forward planning was not found to predict behaviour over and above shallow mentalisation; the model captured beliefs about the selves' immediate reward versus the long-term group reward.

To our knowledge, such Group Mentalisation models have yet to be applied to psychiatric phenomena, despite the likely importance of group-level cognition in a range of psychopathological states. For example, in game theoretic tasks, perceived group cohesion increases paranoid attributions of intent towards groups of opponents [93]; in the Cyberball task, those at clinical high risk for psychosis show higher sensitivity to attributing paranoia when socially excluded [94]; using a public goods game, youth show high levels of co-operation but at the expense of being vulnerable to exploitation [95].

Future directions for formal theories of social representation in psychiatry

Any disorder that impacts cognition might lead to social disability. However, we suggest two components of psychopathology where computational social representation models could make a particular contribution. This is owing to their specifically representational nature and their evidenced role in distress and impairment.

The first is explaining the role of maladaptive schemas in psychiatric disorder. Schemas are high-level cognitive structures that consist of memories, models and action plans that relate to the self, the world, and others and which are developed during childhood and are updated through experience [30, 38]. With respect to theories of social representation [35], schemas may be considered a trait that have down-stream influence on state and action space. The development of maladaptive schemas is strongly linked to adverse childhood experiences [96] and there is good evidence that they are causal factors in depression, anxiety and eating disorders [97]. Importantly, along with their effect in non-social domains, schemas predominantly involve representations of self and others, and these representations are considered key to their causal role in biasing perceptions and actions [35-36]. Although typically conceptualised in descriptive terms, the social representation components of schemas could be captured through formal models that quantify biases in social-value functions. This would require identifying how other-related schema components relate to sensitivity to engage appropriate forward planning and inference across social contexts; learning in the face of uncertainty about others; and sensitivity to identify oneself with a positive group. This procedure would also benefit from longitudinal work to ascertain the impact of abusive or neglectful social environments on alterations to learning in childhood/adolescence, and the resultant maladaptive social representations in adulthood. Previous work [30,98] has suggested ways in which therapeutic mechanisms of interest may be translated into computationally tractable questions; using this foundational work it is possible to make specific predictions around the change of schema in psychiatric disorder using established models (see Box 2).

The second potentially fruitful future target for computational social representation approaches is the experience of illusory social agents in psychosis. Psychotic episodes, common in disorders such as schizophrenia and severe bipolar disorder and occurring after a range of neuropsychiatric difficulties, are notable for the fact that affected people frequently experience interaction with illusory social agents in the form of communication with personified hallucinated voices [99] or have delusional beliefs that involve being targeted by illusory individuals, groups or other unreal social agents [100]. Unlike problems such as social anxiety disorder, where social representations may be distorted but remained tethered to genuine individuals and their actions, in psychosis, the representations of social agents may be internally generated, seemingly sui generis in some cases or after becoming untethered from the genuine social agents with whom they are initially identified and instead begin to be perceived as being autonomous social actors [34]. These experiences are a significant driver of distress [101-102] and now a target for therapeutic intervention [103]. The degree to which humans normally attribute agency in otherwise non-agentive contexts is a matter of continuing investigation (see Box 3). We suggest that computational social representation models have the potential to formally model how illusory intentional agency develops, become untethered from the social environment, is structured, and drives disability. For example, testing whether deeper forward planning is engaged when outcomes are stochastic; a potential marker indicating that intentional agency is being inferred from coincidental outcomes. This frames illusory intentional agency as an identifiable state [37] or process, which may become more frequent under conditions of environmental or physiological stress [104] and may be probed through game theoretic paradigms.

A related consideration is the scope of amodal interactions which we have focused on for characterizing the issues that arise in real-world social dynamics. For example, analysis of eye-gaze and facial displays has been fruitful for uncovering differences in social perception in autism [105]; ecological momentary assessment has offered a granular picture of social and physiological sensitivities in psychosis [106]. Despite the utility of modelling approaches to capture alterations in psychiatric diagnoses such as bipolar disorder, paranoia, and autism cited above, the framework in which we situate our formal models cannot capture all possible naturalistic elements of social interaction. Integrating formal models alongside real-world, naturalistic markers of social interaction may provide a more complete picture of social representation in psychiatric disorder and should be a future goal of the field.

Concluding Remarks

There is a clear need to understand how we structure beliefs about ourselves and others in ways that are amenable to hypothesis-driven cognitive science. Game theoretic tasks can provide controlled paradigms to create socially-regarding scenarios that encourage cooperation, conflict, and evolving social inference, thereby facilitating this approach. Crucially, creating simulations from a specified model can provide normative measures of social interaction to assess individual deviation (e.g. away from normative forward-planning under different social contexts). This latter property allows for the testing of core descriptive clinical theory that captures rich phenomenology of

interest in a shared social environment that can answer questions around the causal processes that go awry in psychiatric disorder.

Nevertheless, we note some potential challenges with the application of computational social representation. The first is the extent to which computational models distinguish between latent representations, which may be causally important but unobservable and even inaccessible to the affected individual, and overt, conscious representations that play a vivid role in mental life. Both are important features of psychopathology, and it is not clear how belief-based models, in principle, can distinguish between them. The issue might ultimately be an empirical one, with hypothesised representations needing to be investigated to test the extent to which they reflect implicit versus explicit social representations as experienced by the patient. Current models of metacognition may be particularly important in assessing this, as they provide a window onto the insight the self has about its own states [107]. It is an open question as to whether metacognitive insensitivity to explicit representations of self may also lead to recursive distortions the self's implicit representations from the perspective of the other.

Secondly, aberrant social representations such as maladaptive schemas and illusory social agents in psychosis are known to evolve in content and accessibility over the lifespan [108-109]. Although this is not an inherent limitation of a computational social representation models, it has not been substantially tested in psychiatry, as most studies have been restricted to brief lab-based tasks rather than being integrated into longitudinal cohort paradigms where changes in social representations over time can be effectively studied [110].

In this review we do not consider biological realisations. Bayesian models, and indeed computational models in general, are abstractions that make precise predictions and provide formal explanations of cognitive processes. How faithfully neural processing hews to the approximately Bayesian precepts that we have articulated is an important, but unanswered, question across many areas of cognitive science [111-112]. Nevertheless, computational models and in silico 'lesion studies' simulating psychiatric dysfunction may still have the capacity to constrain explanations at lower levels, implying their relevance for understanding biological mechanisms [113]).

Finally, the impact of task engagement and comprehension when estimating the approximated beliefs of participants may not be immediately apparent; this is especially true in cases where cognitive impairment is common (e.g. in schizophrenia) and may confound parameter estimates and task performance. Careful consideration must be made within task design to ensure factors such as general cognitive function, attention, and comprehension are controlled for, or model outcomes are compared across patient groups to demonstrate specificity of model predictions, experimental manipulations and reliability (see Outstanding Questions).

Formal models of social representation provide a tractable scientific tool to assess a range of social representations that have been cited as centrally important in a myriad of psychiatric disorders. We believe computational modelling of social representation

can provide a precise, clear, and detailed framework with which to assess some of the most complex social phenomena in psychiatry, and that it may enrich prior work on the representation of minds [35] to explain higher level abstractions implemented in social neurocognitive processes.

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Outstanding questions

- How do mechanisms of basic value-learning contribute to social representation?
 Creating carefully designed within-participant causal experiments can test how specific disruptions to basic value-learning alter the development of novel social representations of interaction partners.
- How stable are parameter and model estimates within computational models of social representation? Estimating the prior beliefs of self and other with a social representation model requires that experimenter's approximations of parameters are reliable, and that winning models are differentiable from other alternative models on recovery. Ensuring recoverability and robust fitting procedures is essential. Stable estimation then allows for the tracking of fluctuations of selfother representations during longitudinal measurements.
- Do parameter estimates from multiple formal models of social representation cluster provide a 'social fingerprint' that defines intra-individual distortions to self and other representation? Considerations include the reliability of models and socially-regarding tasks within-participants, rigour in model fitting procedures, and the need to gather large, high quality sample sizes to detect small effects.
- How can computational models of social representation fit within current dynamic theories of mental disorder? Network and dynamic systems models of psychopathology suggest that disorders are self-maintaining networks of symptoms. Given that altered social representations are likely important in psychopathology, understanding how parameters within social representation models feedback and interact with each other is crucial.
- When do we make agentive attributions in non-social contexts? The extent to
 which we perceive agency or explicitly use the 'intentional stance' to interpret
 non-social situations is currently not well understood and may question our
 assumption that non-social tasks are necessarily devoid of social processing.

[Box 1] Tasks to assess social agent representation

To test social decision-making, experimental frameworks must accommodate social-regarding, multi-person decisions, that is, where decisions involve outcomes for the self and the interacting other(s). This allows the experimenter to capture more ecologically valid ways of how selves come to know other minds in everyday life encounters [114-115] rather than only relying on private, 'spectator' states which may have a minor emphasis on how humans come to know others [116].

Microeconomic games have been used to create carefully controlled socially-regarding situations, where a self's actions influence themselves and other(s), that allow for cooperative and competitive outcomes and have been cited as particularly useful tools for probing interpersonal distortions in psychiatric disorders [13]. Game theoretic concepts can be operationalised within socially-regarding tasks can offer a substrate for mathematically transparent maps from objective value utility to subjective outcomes.

Iterative game theoretic tasks allow the experimenter to study how selves make sequences of social-regarding decisions over time. For example, in one version of the trust task we describe in the text, selves act as investors, and each round, send a sum of money from an endowment to an other. The experimenter triples the money as it transfers to the other, who then decides, as a dictator, how much to send back to the self. The roles could also be reversed. Optimising outcomes in the trust task generally requires selves to build and exploit a predictive model of how the other might feel and act in response to the self's choices, and therefore the behaviour of the self is tied to inferential processes and down-stream strategic considerations (what might the other feel and then do if I send less money; [74]). Some iterative game-theoretic tasks have separated choice behaviour and social inference from strategic goals. For example, using a repeated Dictator game, selves are asked to infer the true intentions of their other after each other decision (cf: [56]). Despite joint outcomes, the other is unable to view the self's attributions, which are therefore observed free from strategic repercussions.

Repeated tasks have also been useful to track social belief change over time, for example in social-value orientation (SVO) tasks (cf: [65]), where alternation between self-guided and other-guided decision making allows experimenters to estimate how a self's individual-level beliefs influence their estimations of a social other's SVO.

[End of box]

[Box 2] Simulating a social exchange to test psychiatric theory

Theories on the effect of early trauma on later risk of developing psychopathology have variously suggested that it disrupts certainty about the sense of self [117] leads to overcertainty about threat from others [118] or leads to maladaptive schemas that can represent a range of pathological beliefs about the self and others [30,98].

Ways in which descriptive therapeutic questions may be translated into computational terms for specific hypothesis testing have been suggested [30]. This work highlights how experimenters can operationalise descriptive theories using computational models that place distinct theoretical, statistical bounds on the uncertainty around how a self may represent themselves and the intentions of a social other, and the interaction of both on future beliefs about the self. For example, experimenters can then test whether those who have been subject to early life trauma attribute greater uncertainties to the self (and self-regarding values), and/or attribute greater uncertainties to representations of others and their intentions. The relationship of changes to structural representations of the self, and subsequent neural and physiological function may then become a more tractable question to answer [119].

To illustrate, we outline a model that defines the joint probability of a self-valuing money for themselves, the probability of the self-valuing equal monetary outcomes, and the self's beliefs about what the other believes along the same dimensions [65], in an interaction involving the risk of personal loss and joint payoff outcomes. The model can also be extended to assess how much a self's representations have changed after exposure to the other (see [60]) to test the impact of the interaction itself.

Simulations indicate how outcomes would operationalise verbal theories from the literature (Figure I). Disruptions to the uncertainty of a self's beliefs about their own social preferences leads to more stochastic outcomes when the self is the decider, and subsequently greater shifts in beliefs following exposure to an interaction other. On the other hand, disruptions to the precision of a self's beliefs about the interaction other leads to poor predictive accuracy, suggesting an inability to successfully model others. Dynamic partner behaviour, based on the experimenter's estimate of self-preferences in phase 1, or partners created based on the behaviour of clinical populations [e.g. 76], may also allow well-controlled predictions and efficient inference about participants as in a form of optimal experimental design. The failure of the model to capture predictions from verbal theories should drive revision of these hypotheses.

[End of box]

[Box 3] Agency and intention in sociocognitive tasks

How are social cognitive processes involved in interactions with intentional social agents? In the lab, experimenters can compare conditions where others believe that they are interacting with an other that is either a person or an algorithm [120] or test two or more people during interpersonal exchange [121]. In online studies, coordinating genuine social interaction is potentially more challenging. One method is to use 'live' social tasks that match participants in real-time although this can require complex software to support this. Another method uses asynchronous 'ex-post matched' designs where selves respond to genuine decisions collected from others taking part at other times [122]. This is more convenient for experimenters but limits the degrees of freedom in the paradigm to ensure the full range of responses is available for later matching.

Interactive paradigms are important, however, as prior work has found that social cognitive processes may be differentially deployed when selves are, or believe they are, interacting with an intentional agent compared to an algorithm as other. This has led to the hypothesis that there may be a process of interpretation that leads people to deploy a 'social' or 'non-social' framework that determines which cognitive resources are applied to a task [120,124].

A related issue is why humans frequently perceive the presence of intentional agents when there is none, or adopt the strategy of acting in accordance with the idea that an interaction may be intentional, even in a range of non-intentional situations? Indeed, humans attribute agency readily to non-social objects that appear to mimic a behavioural policy, for example, where participants attribute intentions to animated shapes [124-125]. Anthropologically, an approach to understanding the world focused on the role of unseen, intentional agents has been noted as a common factor across religions [126]. In psychopathology, the over-perception of external social agency to the point of distress and disability is a key experience of psychosis [34] and has been found in studies that test attribution of agency in the psychosis-spectrum [127-129]. This raises the question of whether people with psychosis systematically mis-deploy a combination of agentive inference (i.e., misdeployment of DoM) and maladaptive social representations (e.g. high weight placed on inferences of harmful intent) in non-intentional contexts.

[End of box]

Table 1. Summary of models of social agent representation. Classes of model are concerning the overall generative purpose. The type of model describes whether the purpose of the model is to detect social regarding (the actions of the participant and/or the partner influence joint outcomes) or non-social regarding outcomes (actions of the participant and/or partner do not influence joint outcomes).

Class	Туре	Ostensive Purpose	Reference
sDoM	Social regarding	The likelihood of harmful intent and self-interest attributions being emitted in response to an other's decisions in a repeated Dictator Game	Barnby et al., 2020 [57]; 2022 [58]
sDoM	Non-social regarding	Estimate the degree to which humans use a Bayesian inverse planning process to predict the actions of an intentional, rational agent	Baker et al., 2009 [49]; Baker et al., 2011 [50]; Baker et al., 2017 [51]
sDoM	Social regarding	Approximate the magnitude and uncertainty of a self's trust beliefs about interacting others given the investment of the other	Lamba et al., 2020 [55]
sDoM	Social regarding	Approximate the changes to belief about self-esteem in response to social evaluation.	Low et al., 2022 [53]
sDoM	Non-social regarding	Integration of facial and utterance trust-cues on emotional inference.	Ong et al., 2015 [52]
sDoM; multi- phase design	Social regarding	Approximate the social-value preferences for absolute and relative payoff of a self, and a self's belief about the preferences of an interaction other.	Barnby et al., 2022 [65]
sDoM; multi- phase design	Non-social regarding	Estimate the change in monetary preferences of the self following exposure to an other using a Delegated Interpersonal Discounting Task (Nicolle et al., 2012).	Moutoussis et al., 2016 [60]
hDoM	Social regarding	Estimate the mentalisation depth of selves. The model allows recursive estimation of a self's strategy, and the strategy of their other within a 'centipede' game	Doshi et al., 2012 [70]; Doshi et al., 2014 [71]
hDoM	Social regarding	Estimate the mentalisation depth of selves. The model allows recursive estimation of a self's strategy, and the strategy of their other within a 'Hide and Seek' game	Devaine et al., 2014 [82]; D'Arc et al., 2020 [83]

hDoM	Social regarding	Estimate the utterances of a speaker to signal utility of semantic meaning for a listener, and the listeners model of the speaker's intentions.	Goodman & Frank, 2016 [72]; Scontras et al., 2021 [73]
hDoM	Social regarding	Generate the choices of a self in an iterative trust task, conditioned on the beliefs of the self and their beliefs about their other.	Ray et al., 2008 [75]; Hula et al., 2015 [47]; Xiang et al., 2012 [74]
hDoM	Social regarding	Estimate a 'game theory of mind' that allows recursive estimation of a self's strategy, and the recursive strategy of their other given the evolving conditions of the Stag Hunt task.	Yoshida et al., 2008 [79]; 2010a [80]; 2010b [81]
Group Mentalisation	Non-social regarding	Estimate the likelihood of differential group membership of several others during a choice preference task	Gershman et al., 2017 [90]; Lau et al., 2018 [87]
Group Mentalisation	Social regarding	Estimate the individual and group utility of investment, and higher-order probability of other group members free-riding.	Khalvati et al., 2019 [91]; Park et al., 2019 [92]

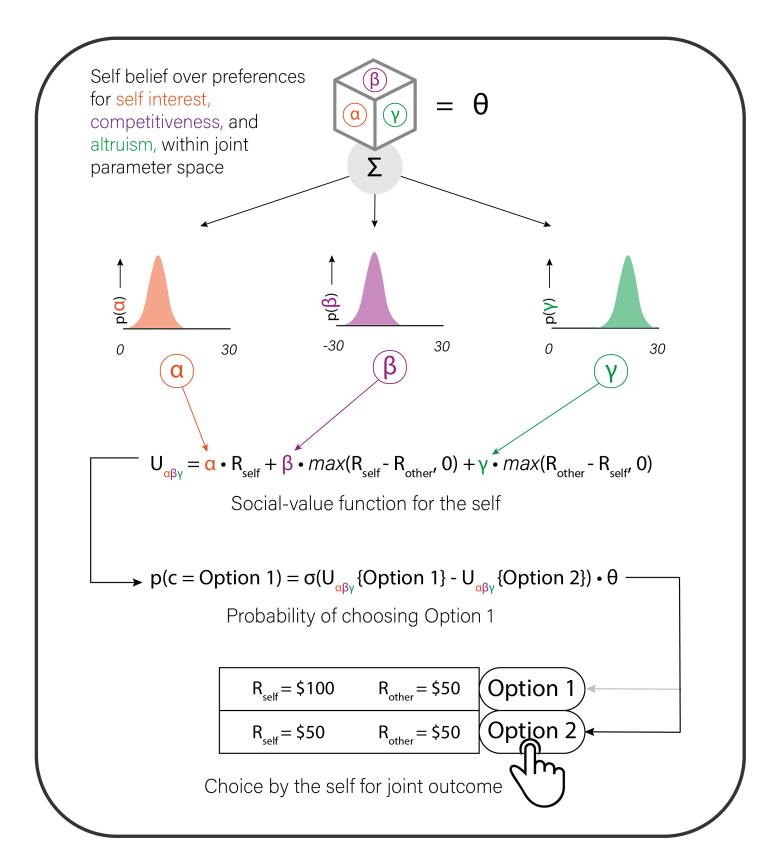


Figure 1. How rich representations of the self translate into joint social action.

Social representation models can hold rich components that represent self and/or an other(s) social-values. By placing probability distributions over state space, social representation models can make predictions about how a self may act in each social environment where outcomes determine joint rewards for the self and an other. In this example, drawing from a Fehr-Schmidt model [130], we demonstrate how self-beliefs (θ) that contain the subjective self-valuation of absolute self-reward (α) , and relative rewards of inequality aversion (β) and altruism (γ) may form an action probability when combined with the difference in utility of choosing Option 1 or Option 2 across the entire state space. In terms of implementation, joint values of self-beliefs (probability distributions over state space) and state-space (values with a range accommodating variables of psychological interest) are both encoded as separate three-dimensional matrices. Self-beliefs along each dimension (α , β or γ) can be calculated by summing (marginalising) along each axis. Importantly, the FS equation is only itself part of the explanation; it specifies the additional model components that provide the causal model structure around the function. Our illustration depicts internal distributions placed over the FS equation; rather than a fitting procedure, it allows experimenters to estimate the uncertainty a self may hold over their own social preferences. In conjunction with other model elements (e.g. social recursion in hDoM, or bias terms in sDoM) and probabilistic distributions, the FS equation can become part of an explanatory theory of cognitive processes. σ = the sigmoid function, c = choice, and therefore p(c = Option 1) = the probability of choosing Option 1.

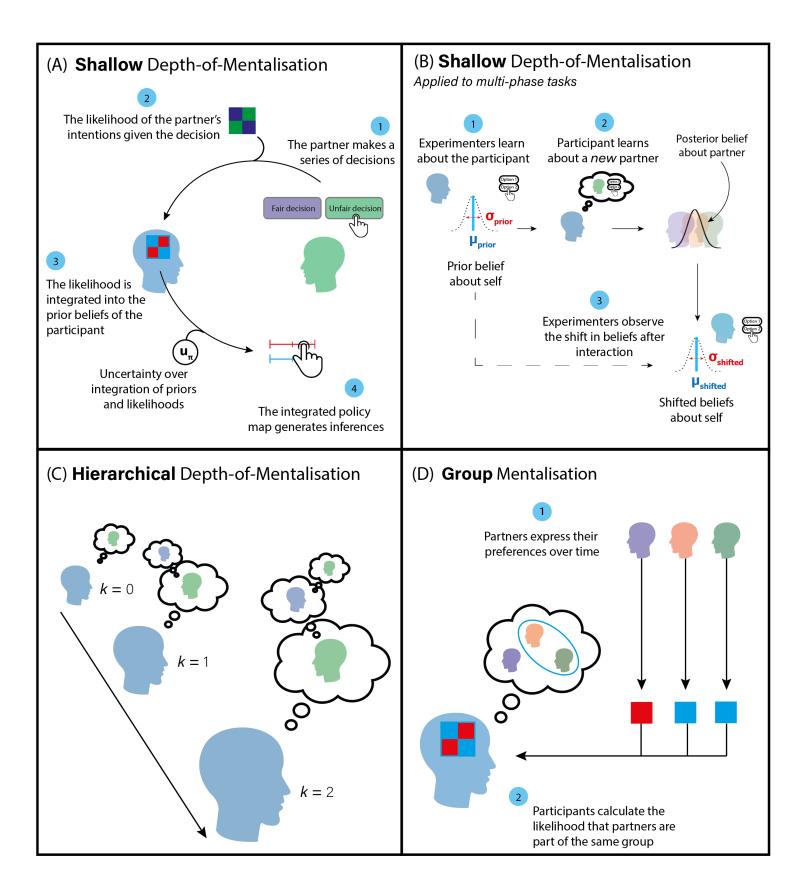


Figure 2. A taxonomy of computational social representation

(A) A schematic of Shallow DoM models with recursive depth $k \le 0$. In this example, the experimenters first learn about the magnitude and uncertainty of a self's beliefs about the intentions of the general population. The self then approximates the likelihood about the intentions of the other given the other's decisions. (B) Shallow DoM models can be used in inter-temporal tasks to assess changes to the representation of the self and other social agents. The experimenter's beliefs over the preferences of the self and the self's beliefs about the other can provide a basic scientific tool to test how the self and other are statistically represented, and what may perturb these representations. In this example, the experimenters first learn about the magnitude and uncertainty of a self's beliefs. The experimenters can then use the self's predictions about the other to build a possibly approximate model of the self's beliefs about the preferences of the other. (C) Hierarchical DoM models (k > 0) allow selves to make recursive inferences in their model of an other, and the model an other may hold about the self, up to level k (in one flavour, assuming that the other is level k-1; in another flavour, that the other is level -1...k-1 or 0...k-1, with a prior probability for each such level). (D) Group Mentalisation models are affiliated with the inferences and social behaviours of the group. This may be non-socially regarding (e.g. group classification based on an other's private preferences) or socially regarding (e.g. the probability of defection in a PGG based on the group's prior history).

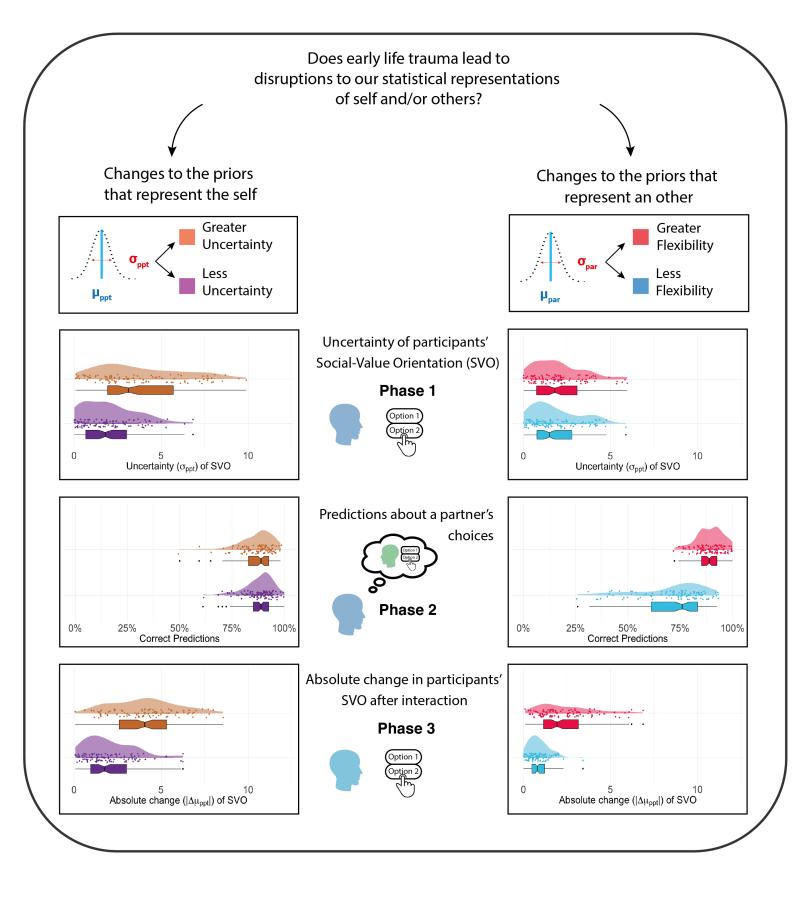


Figure I. Simulations to test changes in self-other representations

Simulating perturbations to the generative process can make firm predictions to formally assess competing hypotheses. Here, synthetic participants are playing an extended social-value orientation (SVO) task. Participants are matched with three different anonymous interaction partners over different phases; one per phase (see [44]). In the phase 1, participants need to decide how to split money with their interaction partner over a series of trials; this is governed by a magnitude (μ_{ppt}) and uncertainty (σ_{ppt}) over self SVO. In phase 2, participants need to guess their new interaction partner's decisions as accurately as possible; this is governed by flexibility around a self's beliefs about an other's SVO (σ_{nar}), where greater values represent a greater ability to step away from self SVO to accommodate the other's SVO. Phase 3 allows estimation of changes in SVO of participants' following exposure to their interaction partner following the interaction of distributions in phase 1 and 2 (see [65]). Right column: Uncertainty does not differ between groups in phase 1. In phase 2, the blue group find it much harder to learn about their partner (fewer % correct). In phase 3, the blue group's SVO is shown to be very rigid compared to the red group (lower absolute change in a self's SVO; $|\Delta\mu_{vvt}|$). Left column: In phase 1 there is larger uncertainty self-SVO in the orange group. However, both groups are good as predicting their partner in phase 2. In phase 3, due to their higher uncertainty over their own SVO, the orange group is highly influenced by their interaction partner versus the purple group.

Glossary

Social Representation: Mental information-bearing structures that organise knowledge about the internal states of others, and the relationship of others to the self; they involve the dynamic interaction and transitions between traits, states, and actions [34].

Computational Model: A set of mathematical equations that determine the flow of information (e.g. beliefs \rightarrow actions) given their structure and interdependency. A computational model can *generate* the actions of an agent given values that determine the solution of each equation.

State Space: A span of independent latent values (S) that determine action probabilities and outcomes (O): $p(O^t|S^t)$. This provides a basis for an agent to form beliefs within the context at hand. State spaces may be continuous (e.g. 0-30) or discrete (0,1) and contain transition structures that determine when an agent moves from one state to another: $p(S^{t+1}|S^t)$.

Reinforcement Learning (RL): An associative formulation that determines the interface between an agent's beliefs and actions. RL models typically describe updates about the inferred value (V) of different stimuli over time (t), and use the difference between expected and actual outcomes (δ) to drive learning about environments:

$$V^{t+1} = V^t + \alpha \delta$$

 $\delta = V^t - Reward$
 α : learning rate

Artificial Neural Network: A collection of interrelated nodes, inspired loosely by biological neurons. Artificial nodes connect to one another using inputs and outputs, where inputs may be raw data (e.g. pixel colour within an image) or the weighted output of another node. Nodes generate probabilistic outcomes using mathematical functions (e.g. SoftMax) to transmit information.

Attractor State Model: Attractor states are cast as hubs generated by dynamic interplay of units within neural networks; over time, small networks units generate the ability to influence a larger proportion of units within a system. In psychological systems, this can be framed as the influence of nodes within a dynamic network.

Bayesian Model: A computational model that involves the interaction of priors and likelihoods combined to form posterior beliefs about the chance of an event occurring. Beliefs in these models are not necessarily propositional attitudes, as defined in the philosophy of personal belief, but rather 'effective' beliefs. In other words, beliefs are probability distributions over *a priori* qualitative dimensions necessary for performing approximate probabilistic inference.

Prior: The initial belief(s) before any evidence has been considered, e.g. the starting probability an other is prosocial: p(Prosocial).

Likelihood: the probability of observations given a set of prior beliefs, e.g. the probability a prosocial other made a competitive decision to split some money: $p(D_{competitive} | Prosocial)$.

Posterior: the product of the likelihood and the initial belief(s), normalised by the marginalised sum of the product to form a new belief, e.g. the probability an other is prosocial given their recent competitive decision: $p(Prosocial|D_{competitive}) =$

 $p(D_{competitive} | Prosocial) \times p(Prosocial)$

 $\frac{1}{\sum p(D_{competitive} | Prosocial) \times p(Prosocial)}$

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