Comparing Theories with the Ising Model of Explanatory Coherence

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Abstract

Theories are among the most important tools of science. Lewin (1943) already noted “There is nothing as practical as a good theory”. Although psychologists discussed problems of theory in their discipline for a long time, weak theories are still widespread in most subfields. One possible reason for this is that psychologists lack the tools to systematically assess the quality of their theories. Thagard (1989) developed a computational model for formal theory evaluation based on the concept of explanatory coherence. However, there are possible improvements to Thagard’s (1989) model and it is not available in software that psychologists typically use. Therefore, we developed a new implementation of explanatory coherence based on the Ising model. We demonstrate the capabilities of this new Ising Model of Explanatory Coherence (IMEC) on several examples from psychology and other sciences. In addition, we implemented it in the R-package IMEC to assist scientists in evaluating the quality of their theories in practice.

Keywords: Theory Appraisal, Theory Development, Explanatory Coherence, Ising Model

Comparing Theories with the Ising Model of Explanatory Coherence

1 Theories are among the most important tools in science. They help scientists to
2 explain and organize knowledge (Vaidyanathan et al., 2015). They motivate the search for
3 discoveries (Smaldino, 2019) and help us to plan interventions by predicting what would
4 happen under hypothetical conditions (Borsboom, 2013; Fried, 2020). In addition, findings
5 that are based on strong theory are more likely to replicate (Oberauer & Lewandowsky,
6 2019). Lewin (1943) put it briefly as “There is nothing as practical as a good theory” and
7 (Thagard, 1988, p.33) summarized it concisely as:

8 Scientific theories are our most important epistemic achievements. Our knowledge of
9 individual pieces of information is little compared to theories such as general
10 relativity and evolution by natural selection that shape our understanding of many
11 different kinds of phenomena.

12 Let us be a bit more explicit. A good scientific theory, such as *evolution through natural*
13 *selection*, reaches far beyond what we have observed or tested. A few elegant hypotheses
14 (see section “Comparing Creationism and Darwin’s Theory of Evolution” for details)
15 explain the entire intricacy, diversity, history, and future of biology. For instance, it
16 explains why there are different species, why whales and mammals that roam the land have
17 comparable skeletal structures, how we can domesticate plants and animals, why blue-eyed
18 parents never have brown-eyed children, why some families have a higher than average
19 proclivity to heart disease, why over hundreds of millions of years most species have gone
20 extinct, why Homo Sapiens has an appendix, why two different species cannot mate, why
21 many but not all species reproduce through sexual intercourse, and how something as
22 complex as binocular vision through photoreception could have evolved from unicellular
23 animals. The theory of evolution also informs us in our development of, for instance, more
24 resilient and nutritious crops and assists us in our fight against heritable diseases, viruses,
25 aging, and death. The theory reaches far beyond what we are familiar with. It allows us to

speculate about life on other planets that are nothing like our own —planets such as Jupiter or Venus— and reason through the possibilities for non-carbon-based or gaseous lifeforms. In short, only a relatively few interlocking hypotheses that constitute the theory of evolution explain the entirety of terrestrial biology and beyond.

However, instead of having such strong theories like *evolution through natural selection*, close to all areas of psychology are characterized by weak theories or a complete lack of theories (Fried, 2020; Oberauer & Lewandowsky, 2019). Such weak theories make imprecise predictions, often hold implicit assumptions, and are sometimes even contradictory (Borsboom, 2013; Oberauer & Lewandowsky, 2019). These problems have been discussed for decades (e.g., Gigerenzer, 1991; Meehl, 1978) and the interest in work on improving in theory is currently increasing (e.g., Borsboom et al., 2020; Fried, 2020; Guest & Martin, 2020; Haslbeck et al., 2019; Kellen, 2019; McPhetres et al., 2020; Muthukrishna & Henrich, 2019; Oberauer & Lewandowsky, 2019; Robinaugh et al., 2020; Robinaugh et al., 2019; Sanbonmatsu & Johnston, 2019; Smaldino, 2019; van Rooij & Baggio, 2020; van Rooij, 2019).

Given the long history of discussions about the need for improved theory and the comparatively little progress that has been achieved, it is important to reflect on the reasons for this situation. To assist us, let's liken theory development to navigation without a map towards a desired destination. Navigation is difficult to nearly impossible without either points of reference or instruments (e.g., compass, sextant, GPS). Unfortunately, points of reference (empirical results) are generally far from specific and unambiguous in psychological science, because, the subject matter (e.g., intelligence) is not directly observable and fine-tuned experimental manipulation and control is difficult (or unethical). However, thus far, most attention has been allocated to the improvement of empirical research methods (e.g., preregistration, open science, increase in statistical power, improvement in measurement; e.g., Nosek et al., 2018; Vazire, 2018). The improvement in research methods has shown clear benefits, though better scientific theories have not been

one of them. Hence, we believe that systematic theory assessment tools (i.e., the equivalent of GPS or sextant) are required if we want to evaluate and move towards better scientific theories (Borsboom et al., 2020).

One of the avenues we see for such tools is the assessment of the coherence between the constituent components of a theory (e.g., Haig, 2005; Poston, 2021; Thagard, 1989, 2007). A case could be made that at least part of the success of a strong theory such as *evolution by natural selection* is related to how well the theory's components interlock. Like a well made watch where all the gears, wheels and springs are made to minute precision to give rise to robust timekeeping without 'time' being a part of any of the components. Removing or changing a single gear would radically change its behavior.

Like in a watch, the coherence of a theory's components is of vital importance. To clarify this claim, imagine one of our earlier explanations of the seasons.¹ In ancient Greece, it was thought that winter was caused by the goddess Demeter taking the warmth from the earth, because of her grief for her Daughter Persephone spending six months with her husband, the god Hades, in the underworld. The problem with this theory is not that it fails to explain the lack of seasons on the equator and reversal of the seasons on the other hemisphere. The problem with this theory is that all its components can be changed without affecting the results. For instance, the gods could be completely different, the reasons for taking the warmth away could be different, or even more fundamental changes, such as bringing warmth instead of taking it away or removing Persephone and Hades from the story, would not have to change anything in the end result of seasons.²

¹ The example that follows is a paraphrasing of the example given by David Deutsch in his inspiring book *The Beginning of Infinity* (pages 19 through 25).

² This example was chosen for narrative purposes. We acknowledge that some might consider this example naive or unscientific. Please note that this example can easily be replaced by *intelligent design*, the *élan vital* theory, *ego depletion*, or many others that were considered scientific at some point in history.

On the other hand, the conventional theory of seasons does not have any components that can be changed without major repercussions. As we know it, a) heat radiates from the sun; b) the earth is a sphere that periodically rotates around the sun and around its axis; c) the axis of the earth is tilted and through this axis tilt, the radiation of the sun hits the earth at an oblique angle; d) the atmosphere of the earth shields its surface from a certain amount of the radiation depending on its density. When these components are combined, winter on the northern hemisphere is when, during earth's revolution around the sun, the northern hemisphere is tilted away from the sun, the sun's radiation travels a longer distance through the earth's atmosphere, and thus is heating the surface in a smaller amount. This *axis-tilt theory of seasons* explains why there are annual seasons, why there is a half-year difference between the northern and southern hemispheres, and why there are no seasons on the equator. Removing or changing one of the components of the theory would have drastic consequences; the annual seasons as we know them would not arise. In brief, strong scientific theories show a high degree of *explanatory coherence* (Thagard, 1989) between its constituent components, which could thus be considered an informative quality to assess.

Consequently, we provide a tool to systematically assess the explanatory coherence of scientific theories. In this article we outline the argumentation for and explain the application of our straightforwardly usable tool *IMEC*, which we implemented in R (Maier, 2020).³ In the next sections, we first explain the difference between data, phenomena, and theory since this is a key distinction in our approach. This is followed by an explication of the theory of explanatory coherence (TEC), a way to assess the quality of a theory based on establishing principles (Thagard, 1992). On this foundation, we develop a new implementation of TEC, the Ising Model of Explanatory Coherence (IMEC). In the second to last section, we exhibit the use of IMEC and how it expresses desirable theoretical

³ To facilitate application in practice, we also implemented our new method in the R package. A tutorial for fitting IMEC in R can be found at <https://osf.io/j4uvw/>.

qualities. Specifically, we first demonstrate that uncontroversial theoretical qualities (e.g., simplicity) are embodied by IMEC. Second, we compare two different theories explaining the *positive manifold of intelligence* either by mutualism or a common (latent) cause, to show how IMEC can be used to compare different psychological theories and identify critical experiments. Third, we compare *intelligent design* (formerly known as *creationism*) to *evolution by natural selection* to illustrate how the explanatory coherence of a theory is influenced by alternative explanations.⁴ The paper is concluded with a discussion of the limitations and suggestions for further development and research.

Theory, Phenomena, and Data

For our method, we rely on a distinction between data, phenomena, and theory (Bogen & Woodward, 1988; Haig, 2005; van Rooij & Baggio, 2020; J. F. Woodward, 2011, Figure 1). In this distinction, *data* are structured representations of observations that can provide evidence for phenomena. In psychology, typical data are reaction times, error rates, responses to multiple-choice questions, and scores on Likert or visual analog scales. *Phenomena* are general and stable features of nature, which scientists seek to explain (Bogen & Woodward, 1988; J. F. Woodward, 2011; J. Woodward, 1989). We tend to identify phenomena as general patterns in data —structures that are observed across datasets— which, in psychology, are often called ‘effects.’ A prime example of a phenomenon is the *Stroop-effect* (e.g., MacLeod, 1991). The Stroop-effect is the general pattern that people take longer to classify the color of a word when the word spells an incongruent color. To evaluate the relationship between data and phenomena, researchers usually use statistics. For example, a significant interaction between condition and reaction time/error rates in a within-subject ANOVA could indicate evidence for the Stroop-effect. *Theories*, on the other hand, do not directly relate to the data but explain existing phenomena and motivate the search for new phenomena. For example, *automaticity*

⁴ More example applications can also be found in the appendix.

—people need to suppress the automated reading of a word— is a theory that explains the phenomenon that reaction times are longer in incongruent trials. A theory can be considered a set of hypotheses⁵ that collectively explain the phenomena. In the case of automaticity, one of its hypotheses would be that suppressing an automated processes requires attention, and thus time, which explains the longer reaction time for incongruent tasks.

The process of moving between theories, phenomena, and data can be seen as an inference cycle (Figure 1). From theories, we can deduce phenomena that nature should exhibit if our theory is correct. These phenomena in turn give use predictions about what patterns we should observe in data from observation and experimentation. In turn, from particular datasets that share common patterns, we can generalize to phenomena. From phenomena, we can conjecture a theory about how nature is that would explain these phenomena (i.e., abduction; Haig, 2005; Peirce, 1958; Thagard, 1992; Thagard & Nowak, 1988). As scientists, we would like to evaluate how well data, phenomena, and theory are connected. Applied statistics offers an abundance of techniques to evaluate the extent to which phenomena are supported by the data. However, few methods exist for appraising how well phenomena support or follow from theories.

The Theory of Explanatory Coherence

Thagard (1989, 1992) proposed such a theory appraisal method; a systematic way to compare different theories based on *explanatory coherence*. Explanatory coherence is a concept devised to capture several considerations of scientific reasoning when appraising theories. It is geared towards capturing a theory’s consistency with established theories and the breadth of what a theory is said to explain (i.e., number of phenomena), which is in turn constrained by its simplicity. This embodies crucial aspects that correct theories

⁵ Note that these are substantive/explanatory hypothesis of the kind ‘organic being undergo natural selection’ and are not to be confused with statistical hypothesis.

Figure 1*Relationship Between Theory, Data, and Phenomena.*

148 agree, that theories should not be too simple and thus fail to explain anything and that
 149 theories should be penalized for the addition of ad-hoc assumptions to explain more
 150 phenomena (Thagard, 1989, 1992).

151 For explanatory coherence, a theory consists of a set of explanatory hypotheses that
 152 explain a set of phenomena that are supported by empirical research. Within this
 153 framework, the evaluation of a hypothesis is based on the number of explanatory relations
 154 to other hypotheses or claims about phenomena. For example, if a hypothesis explains
 155 multiple phenomena, it should be preferred over a hypothesis that explains only one
 156 phenomenon. Let us illustrate this using the Stroop task and attention example from

above. The fact that suppressing an automated processes requires attention, not only explains longer reaction times on incongruent trials, but also higher error rates as well as impaired performance under high cognitive load (MacLeod, 1991). This makes it preferable over a theory that would need to postulate different hypotheses to explain each phenomenon separately. To capture intuitive principles like these, (Thagard, 1989; revised in Thagard, 1992) postulated seven principles which give rise to the explanatory coherence relationships. From these explanatory coherence relations the theory appraisal considerations “follow as a matter of course.” These principles form the (meta) *theory of explanatory coherence* (TEC).⁶ We quote these seven relations from as described in Thagard (2000, p.43):

1. **Symmetry.** Explanatory coherence is a symmetric relation, unlike, say, conditional probability. That is, two propositions p and q cohere with each other equally.
2. **Explanation.** (a) A hypothesis coheres with what it explains, which can either be evidence or another hypothesis. (b) Hypotheses that together explain some other proposition cohere with each other. (c) The more hypotheses it takes to explain something, the lower the degree of coherence.
3. **Analogy.** Similar hypotheses that explain similar pieces of evidence cohere.
4. **Data Priority.** Propositions that describe the results of observations (usually claims about phenomena) have a degree of acceptability on their own.
5. **Contradiction.** Contradictory propositions are incoherent with each other.
6. **Competition.** If p and q both explain a proposition, and if p and q are not explanatorily connected, then p and q are incoherent with each other (p and q are

⁶ These seven principles can also be seen as meta-hypotheses, which can in principle be tested and evaluated like regular hypotheses.

179 explanatorily connected if one explains the other or if together they explain
180 something).

181 **7. Acceptability.** The acceptability of a proposition in a system of propositions
182 depends on its coherence with them.

183 In these principles, a proposition is either an explanatory hypothesis of a theory, or
184 a phenomenon, which is to be explained by a theory. The principle of explanation is the
185 most important principle since it establishes most of the explanatory coherence
186 relationships. Acceptance can be considered the dependent variable of TEC, which results
187 from the explanations established by the other six principles. See Thagard (1992) for a
188 detailed disquisition of all seven principles and their origin.

189 Thagard (1989) implemented these principles in a connectionist model called
190 Explanatory Coherence by Harmany Optimization (ECHO).⁷ Connectionist models
191 describe a network with excitatory and inhibitory links between nodes. The different nodes
192 can have varying degrees of activation. Whenever a given node is activated it activates
193 nodes with which it is connected through excitatory links and deactivates nodes with which
194 it is connected through inhibitory links. The degree to which the connected node is
195 activated or deactivated depends on the strength of the excitatory or inhibitory link. In
196 ECHO, two (or more) theories are compared in their explanation of phenomena. The
197 network of these phenomena and hypotheses of the theories is run in several iterations in
198 which nodes update each other according to the connecting links, usually until it settles in
199 a stable state where one theory has a higher activation than the other(s). A detailed
200 analysis of ECHO is beyond the scope of this paper (see Thagard, 1989, 1992).

⁷ To acknowledge Gilbert Harman, who conceptualized inference to the best explanation, Thagard uses the word Harmany rather than the more common word harmony.

ECHO has proven its value in the appraisal of theories,⁸ yet it has two key limitations. The first limitation of ECHO is that, because of the connectionist architecture, it is incapable of appraising individual theories. It can only be used to compare two or more theories. This is because, when only one theory in relation to the phenomena is being evaluated in ECHO, only excitatory links will be established since contradictions (inhibitory links) usually only occur between two competing theories. Therefore, the activation of nodes will increase indefinitely when running the network for several rounds. The system does not settle to a stable state that expresses the explanatory coherence. ECHO's second limitation is that it is not available in any software psychologists typically use, which greatly reduces its usability for theory improvement in psychological science. These limitations prompted us to develop a novel implementation of TEC.

The Ising Model of Explanatory Coherence

We developed our instrument in the common programming language R and implemented TEC using the Ising model (Ising, 1925). This has resulted in an R package **IMEC** that researchers can easily use to appraise the quality of their theories.

Revising TEC

For the implementation of TEC in IMEC, we exclude several of TEC's principles. Specifically, we excluded principles 2b (propositions that explain evidence together cohere), 3 (analogy), and 6 (competition). Thagard (1989) based his principle 2b (part of Explanation) "For each P_i and P_j in $P_1...P_m$, P_i and P_j cohere" on the Duhem-Quine thesis (Duhem, 1954) that explanation or prediction requires a bundle of mutually dependent co-hypotheses and assumptions. However, Thagard (1989, p. 437) already notes problems with this principle. He states "any scientist who maintained at a conference that the

⁸ For instance, it proved its mettle in evaluating key theories from the history of science, such as comparing different theories about why the dinosaurs became extinct or different theories to explain continental drift (Nowak & Thagard, 1992; Ranney & Thagard, 1988; Thagard, 1991, 2005).

theory of general relativity and today's baseball scores together explain the motion of planets would be laughed off the podium. Principle 2 is intended to apply to explanations and hypotheses actually proposed by scientists". There are many more cases where we can find problems with this principle. For example, if a depression is caused by one's physiological predisposition as well as one's life partner dying in a car crash, would this lead us to conclude that physiological predisposition for depression and life partners dying in car crashes cohere? It seems more that two *unrelated* causes together explain the depression. Therefore, we decided not to model principle 2b.⁹

We also decided against modelling Principle 3, Analogy. While analogy often seems to be useful in generating new discoveries, it is not established as a criterion for the quality of a theory. In practice, it is also often hard to differentiate what kinds of explanations are actual analogies and what kinds are illustrative metaphors. Noteworthy for psychology, some theories that were based on analogies or metaphors turned out to be hardly replicable (e.g., Carter & McCullough, 2014). A case could be made that actual analogies, as differentiated from metaphors, increase the approximate truth of a theory. An example is the analogy between artificial selection of traits in the domestication of herd animals and the development of traits in animals through natural selection. However, without giving a detailed explication of what makes something sufficiently count as an analogy, scientists can easily 'boost' their theory's explanatory coherence by tagging on metaphors and selling them as analogies. Such demarcation is beyond the scope of the paper; thus we (currently) did not model analogy in IMEC.

Finally, we excluded Principle 6, the principle of competition "If P and Q both explain a proposition P_i , and if P and Q are not explanatorily connected, then P and Q incohere." This principle seems to be a requirement of the connectionist architecture of ECHO. Namely, if there are too many excitatory links compared to inhibitory links in a

⁹ Researchers who want to incorporate this principle when using IMEC can still do so by manually adding explanatory links between hypotheses that together explain phenomena.

network, then the activation of nodes increases with each iteration and the network does not settle in a stable state. Hence, Thagard (1992) seems to have added the principle of competition to create more inhibitory links. Conceptually, there does not seem to be a strong reason why two propositions that are not explanatorily connected and explain some evidence would incohere. It could even be argued that it is desirable to allow the development of a model of explanatory coherence that does not impose incoherence in order to settle to a stable state. This is desirable, because there are many cases in which explanatory hypotheses of one theory do not contradict the hypotheses of the other theory in their explanation of the same phenomena. For instance, both a sprinkler system and rain are viable explanatory hypothesis for wet pavement, but one does not have to exclude the other. In addition, the absence of an inhibitory link requirement would enable researchers evaluate individual theories.¹⁰

Requirements for a Model That Can Implement the Modified TEC

We are left with five out of seven of TEC's principles. These principles are to be our meta explanatory hypotheses from which the qualities of good theories should follow as a matter of course. We summarize these principles as the following requirements of a model that incorporates TEC:

1. The model needs symmetric connections between hypotheses and phenomena to incorporate principle 1 (symmetry).
2. It must be possible to establish positive as well as negative connections between phenomena and hypotheses to represent principle 2 (explanation).
3. It needs some external force that gives the phenomena some degree of acceptability on their own to incorporate principle 4 (data priority).

¹⁰ Note, researchers that wish to model Principle 6 can still do so by assigning negative connections between the particular hypotheses of the theories.

4. It must be possible to establish negative connection to represent principle 5
(contradiction).

5. It requires a measure for the activation of phenomena and hypotheses to denote
principle 7 (acceptability).

Incorporating TEC in the Ising Model

One model that has these four properties is the Ising model (Ising, 1925). We developed a new computational algorithm to evaluate explanatory coherence based on the Ising model that we term the Ising Model of Explanatory Coherence (IMEC). To understand the proposed method, it is necessary to outline the basic properties of the Ising model.

The Ising model was originally developed in statistical mechanics to describe the polarization of ferromagnetic materials (Ising, 1925). However, its properties are useful to model a variety of systems and the model has been applied widely, for example, to model psychological constructs and opinion dynamics (Dalege et al., 2016; Epskamp et al., 2016; van der Maas et al., 2020). The Ising model describes a binary network in which each node can have states 1 and -1. This can be interpreted as the node being either ‘on’ or ‘off.’ For instance, a person either has a symptom or she does not. The probability of a node being in a certain state is influenced by three parameters (Epskamp et al., 2016).

1. The threshold parameter τ represents the tendency of a node to be in a given state.

The higher (lower) τ , the more the node prefers to be in state 1 (-1). For example, in Figure 2, if we add a threshold of one to node one, this would increase the probability of this node to be in state one. The probability would be 0.881 and, thus, higher than the 0.5 probability of being in state one that we would find without threshold.

2. The network parameter or edge weight ω denotes the pairwise interaction between two nodes. A positive ω between two nodes indicates that they prefer to be in the

same state, while a negative ω between two nodes indicates that they prefer to be in different states. The larger the absolute value of ω the stronger this tendency. In Figure 2 adding the threshold on node one does not only increase the probability of node one to be in state one but also of node two. The reason is that this node prefers to be in the same state as node one because of their positive connection. Thus, after adding the positive threshold to node one, the probability of node two to be in state one is also increased to 0.790.

3. The inverse temperature β determines the entropy of the model and is only of minor importance for our implementation. If β equals zero, the probability of each state is equal, whereas for very high values of β , the network can often be in only one state. Note that β is a scalar on ω and τ and can be modelled using these parameters. In other words, if we divide β by some value and multiply all ω and τ parameters with the same value, we obtain the same probability (Epskamp et al., 2016). For instance, a node with $\tau = 1$ and $\beta = 1$ has the same probability of being in a given state as a node with $\tau = 2$ and $\beta = 0.5$). Therefore, we do not need to model β directly.

Figure 2

A simple example case to illustrate the Ising model.

We can think of the different nodes as propositions in terms of TEC. In other words, each node represents either a phenomenon or a hypothesis in a theory. The relationship between phenomena and hypothesis and their acceptability can then be determined using the principles of explanatory coherence. The pairwise interactions are by definition

symmetric and, therefore, satisfy principle 1 (symmetry). Principle 2 (explanation) and 5 (contradiction) are incorporated through the edge weights ω that allow us to establish positive and negative connections between nodes. In addition to incorporate principle 2 (c) that the degree of coherence is inversely proportional to the number of explanatory hypotheses, we divide the edge weights by the number of hypotheses needed for an explanation (e.g., if two hypotheses are needed to explain a phenomenon the edge weight is half compared to a situation where only one hypothesis is needed to explain a phenomenon). Lower edge weights imply that the hypotheses become less activated if the phenomenon is in state one. For instance, the hypotheses that organic beings have evolved and that organic beings undergo natural selection together explain that the embryos of different species are similar. Third, by putting a threshold τ parameter on the phenomena we can model the impact of evidence, or data priority (principle 4). In the example above, the stronger the evidence for the similarity of embryos of different species, the stronger would be the threshold on this phenomenon. This would also imply that the hypotheses connected to this phenomenon (organic beings have evolved, organic beings undergo natural selection) are also supported more strongly. If there is no specific knowledge regarding the strength of evidence and strength of explanation, we use default settings inspired by Thagard (1989), which are thresholds of two on the phenomena, a weight of one for explanation, and a weight of minus four for contradiction.

Finally, we need a measure for the explanatory coherence, which is manifest in principle 7 (acceptability). This explanatory coherence is the dependent measure of IMEC. Theories with higher explanatory coherence are preferable over theories with lower explanatory coherence. In the Ising model, we can consider the explanatory coherence of a state as the probability that a state occurs. States that are more likely to occur in the Ising model have higher explanatory coherence than states that are less likely to occur.

The probability of a state (i.e., a given configuration of *all* nodes) in the Ising Model can be calculated with the following equation:

$$Pr(X = x) = \frac{\exp(-\beta H(x))}{Z}. \quad (1)$$

Here, Z denotes the sum of $\exp(-\beta H(x))$ over all possible states. $H(x)$ simply denotes the Hamiltonian function. This is a function of the form

$$H(x) = -\sum_i \tau_i x_i - \sum_{i,j} \omega_{ij} x_i x_j, \quad (2)$$

where τ_i denotes the thresholds on the node and ω_{ij} the connection to other nodes for a state x .

The explanatory coherence (defined by principle 7 or acceptability) of a hypothesis can be represented by the probability of a given node to be in state 1. Therefore, we sum $Pr(X = x)$ over all states X where a given node X_k is in state one. The explanatory coherence can be denoted as.

$$ec(X_k) = Pr(X_k = 1) = \sum_{x \in (x_k=1)} \frac{\exp(-\beta H(x))}{Z}. \quad (3)$$

In other words, we calculate the probability of all given configurations in which a hypothesis is true.¹¹ If we look at more than one hypothesis but a set of hypotheses, the explanatory coherence is simply denoted as the *average* over the coherence of the individual hypotheses. Although we use the probability of a given state in the Ising model as the foundation for our method, we want to emphasize here, that the resulting number can **not** directly be interpreted as the probability of a theory being true. Different considerations, such as the role of contradictions, and the fact that we average over individual nodes, when calculating the coherence of a theory complicate this matter. Therefore, the explanatory coherence values should simply be regarded as numbers between zero and one and not as probabilities for the truth of a theory. In the next section we give some aid for the interpretation of these numbers.

¹¹ Note that this explanatory coherence can not only be calculated for hypotheses but also for the claims about phenomena themselves, although they often have higher explanatory coherence due to data priority.

Rule of Thumb for Interpreting Explanatory Coherence

The higher this explanatory coherence is, the better, but how high is enough to actually accept a theory? The question of how to interpret the values for the explanatory coherence of theories requires careful consideration. We do not want to establish a default benchmark. Plenty of problems have been ascribed to blindly following the p -value threshold of 0.05 (e.g., Lakens et al., 2018; McShane et al., 2019) without paying the necessary attention to context (e.g., sample size and effect size). At the moment, we can offer two rules of thumb, one for single theory evaluation and one for theory comparison. In the single theory case, we can derive reasonable values based on the hypotheses : phenomena ratio of simple examples (see Figure 3). This indicates that an explanatory coherence of 0.867 can be considered low, an explanatory coherence 0.950 can be considered medium, and an explanatory coherence of 0.977 can be considered high. However, we want to reiterate that these benchmarks are only meaningful in the single theory case; in the theory comparison case contradictions between theories complicate the picture and these rules of thumb should not be used. In the case of theory comparison, researchers should favor the theory with the highest explanatory coherence. It must be noted that thorough investigation into the behavior of explanatory coherence is required before trustworthy guidelines can be established.

IMEC's Representation of Different Criteria for Theory Evaluation

Next, let us show on four small examples inspired by Thagard (1989) how IMEC smoothly integrates considerations that scientists use for theory evaluation in practice. These are explanatory breadth, refutation, simplicity, and deactivating evidence (e.g., Meehl, 1992, 2002). In the next examples we run IMEC with the default settings based on Thagard (1989). This is a threshold (evidence) of two on the phenomena, positive weights of one for the explanations, and weights of minus four for contradictions. While this setting has been shown suitable in comparing a wide range of cases, there is nothing special about

Figure 3*Rule of Thumb for Interpreting Explanatory Coherence in the Single Theory Case*

Note. Panel A: Low explanatory coherence (0.867); Panel B: Medium explanatory coherence (0.950); Panel C: high explanatory coherence (0.977)

these parameter values. In practice, we encourage researchers to deviate from the default if, for example, one phenomenon has stronger empirical support than others.

Explanatory Breadth

Explanatory breadth, the number of phenomena that a theory can explain, is a criterion scientists commonly use to compare theories. If a theory explains more, it is preferred over a theory that explains less. Therefore, given the same complexity, IMEC should prefer the proposition that explains more phenomena. This setting is illustrated in Figure 4, where H1 gives a broader explanation of observed phenomena and should, thus, be preferable. Let us consider how IMEC evaluates this case. Comparing the two theories with IMEC based on Equation 3 indicates an explanatory coherence of 0.867 for H1 and an explanatory coherence of 0.134 for H2. In other words, IMEC seems to correctly prefer theories of higher explanatory breadth.

Figure 4*Explanatory Breadth*

Note. Blue lines indicate positive connections with weight one, red lines indicate negative connections with weight four and thresholds on the phenomena are set to two.

Refutation

Falsification - the abandoning of refuted proposition - is sometimes considered the defining criterion of science (Popper, 1959). However, in practice scientists do not directly discard an otherwise successful theory after one failed prediction and it is probably also wise not to do so (Lakatos, 1978). The refutation of a theory might often depend more on whether better, alternative explanations become available. Figure 5A shows a setting where a proposition H1 explains two pieces of evidence E1 and E2 but also predicts a phenomenon E3 for which contradicting evidence exists. We use the same thresholds and edge weights as before but assign a threshold of -1 to E3. In this setting, IMEC assigns an explanatory coherence of 0.867 to this hypothesis. In other words, the hypothesis is not directly refuted because of one incorrect prediction. Figure 5B shows the same setting, however, now an alternative explanation H2 has become available which does not predict E3 and contradicts the old explanation. Now, the explanatory coherence of H1 drops to 0.135 and H2's explanatory coherence is 0.867. This shows that the explanatory coherence of a proposition usually depends also on the availability of alternative explanations.

Figure 5*Refutation*

Note. Blue lines indicate positive connections with weight one, red lines indicate negative connections with weight four. Thresholds on the phenomena are set to two for E1 and E2 and to minus two for E3. Note that the blue weights are equal in both figures and are scaled down in figure B only in comparison to the contradiction of weight four.

415 Simplicity

416 Because of principle 2c, the connection between a phenomenon and its explaining
 417 proposition is inversely proportional to the number of explanations. Therefore, if more
 418 propositions are needed to explain a phenomenon, this should result in lower explanatory
 419 coherence, reflecting the principle of simplicity. Figure 2 shows two theories with either one
 420 proposition (yellow) or two propositions (green). Because the green theory needs two
 421 propositions to explain E1 each of them only has a connection of $1/2 = 0.5$ to this
 422 phenomenon.¹² All other weights and thresholds are one or minus one as before. With this

¹² In practice IMEC will do this kind of scaling automatically.

setting, IMEC indicates that the simpler theory's explanatory coherence is 0.722, while the explanatory coherence of the two proposition theory is only 0.500. In other words, IMEC captures simplicity as a criterion for theory appraisal.

Figure 6

Simplicity

Note. Blue lines indicate positive connections, red lines indicate negative connections. The connections from H2 and H3 to E1 are only 0.5 in this setting since they jointly explain this phenomenon. Thresholds are set to two.

Deactivating Evidence

Because of the principle of data priority, phenomena that are supported by evidence have some explanatory coherence on their own as modeled by assigning them positive thresholds. However, if a phenomenon contradicts a variety of well-supported propositions, researchers often disbelieve it or downplay this phenomenon. Let us consider the example in Figure 7. We can see that the phenomenon E1 is connected to the inferior hypothesis H1 that contradicts a better supported hypothesis (H2). All edge weights and thresholds are again set to 1 or -4 (red weights). In this setting, the explanatory coherence for phenomenon E1 is only 0.884 and thus smaller than for the other phenomena (0.995, 0.995,

0.995). In other words, the phenomenon was downplayed since it was only predicted by one very implausible proposition H1.¹³

Figure 7

Deactivating Evidence

Note. Blue lines indicate positive connections with weight one, red lines indicate negative connections with weight minus four and thresholds on the phenomena are set to two.

Example Applications of IMEC

Positive Manifold of Intelligence by Mutualism

The next paragraph shows the usefulness of IMEC as a tool to compare psychological theories by comparing the explanatory coherence of two theories of intelligence, the g-factor explanation (e.g., Spearman, 1904) and mutualism explanation (van der Maas et al., 2006). We also show that IMEC allows to evaluate the robustness of

¹³ Note, if the researcher finds this property of downplaying evidence undesirable, it can easily be prevented by assigning high thresholds to the phenomena.

the theory to weak evidence or weak explanations and to identify critical experiments by thinking through counterfactuals.

Van der Maas et al. (2006) propose an alternative model of intelligence that explains the positive manifold (the positive correlation of different components of intelligence) not by commonly used latent variable explanations (g-factor) but by mutualism. Development by mutualism means that the positive correlation between different aspects of intelligence (e.g., verbal reasoning, logical-mathematical thinking) occurs solely due to positive interactions between several distinct cognitive processes during development. This idea is inspired by ecology, where for example, the correlation between different aspects of water quality in a lake (e.g., vegetation, water quality) is not explained by a “lake-factor” but by the positive interactions between different aspects of water quality (e.g., Scheffer, 1997; Scheffer et al., 1993).

Based on this model, van der Maas et al. (2006) explain a variety of phenomena in intelligence research, some of which latent variable models have struggled to explain for a long time. However, they also introduce some new assumptions (explanatory hypotheses that support the main hypothesis); therefore, it is interesting to investigate whether their new theory has more explanatory coherence than a latent variable explanation.

Table 1 shows different phenomena related to intelligence and the propositions of the mutualism and the g-factor explanations. The explanatory relations can be seen in Figure 8 with edge weights and thresholds based on the default explained above. Looking at the figure shows that it appears difficult to compare these two theories intuitively. The mutualism theory explains more phenomena than the g-factor theory. However, it is also more complex. Hence, an instrument like IMEC that can assess the trade-off between these different epistemic values seems required for effective theory comparison.

Implementing these explanatory relations in IMEC indicates that the mutualism explanation is superior with an explanatory coherence of 0.788, whereas the explanatory coherence of the latent variable explanation is only 0.504; in other words, the mutualism

Table 1*Mutualism versus Latent Variable Explanation*

Phenomena
E1: There exists a positive manifold between test scores.
E2: Intelligence is hard to predict from early childhood performance.
E3: Intelligence can be described by a hierarchical factor structure.
E4: General intelligence is highly heritable.
E5: Jensen Effect - The larger the g-loading of cognitive tests the larger the heritability.
E6: Flynn effect - IQ increased over time.
E7: Differentiation effect - The positive Manifold is not uniform in the population.
E8: No biological variable could be identified as the unitary cause of g
Mutualism Hypotheses.
HM1: Each cognitive process supports the development of other processes.
HM2: Growth can be described by a logistic model.
HM3: There are small genetic intercorrelations of resources.
HM4: Intelligence and environment cause each other reciprocally.
Latent Variable Hypotheses
HL1: Intelligence is caused by a common latent variable.
HL2: Intelligence and environment cause each other reciprocally
<i>Note.</i> Extracted from van der Maas et al. (2006).

hypothesis seems preferable. This exemplifies how IMEC can smoothly compare theories in contexts where it is intuitively hard to decide between theories.

However, van der Maas et al. (2006) state regarding E7 (differentiation effects) that this phenomenon has not been replicated consistently. Differentiation effects imply that the g-factor is not uniform in the population. In particular it has been suggested, that the

Figure 8

Explanatory Relations for the Comparison Between the Positive Manifold Theory of Intelligence and Latent Variable Models of Intelligence.

Note. Corresponding phenomena and propositions can be found in Table 1. The default edge weights are one; however, edge weights are split when multiple propositions are needed to explain a phenomenon. HM1 and HL1 have a strong negative connection of minus four. Thresholds for the phenomena are set to two and to minus two for the phenomenon E8.

positive manifold declines with age (e.g., Tideman & Gustafsson, 2004) and that the positive manifold is stronger in lower IQ groups (e.g., Deary et al., 1996). However, both of these manifestations could sometimes not be replicated (e.g., Facon, 2004). In other words, due to the weak evidence for this phenomenon, we should consider stepping away from IMEC's default settings and lowering the threshold on E7. In addition, van der Maas et al. (2006) state that the mutualism model allows for both differentiation and integration; in other words, the model makes a very general prediction with regards to differentiation effects that can easily be confirmed. Therefore, let us consider what happens if we reduce both the evidence for E7 and the weight between HM1 and E7 from 1 to 0.5. In other words, to account for the problematic state of this phenomenon and the vague prediction of the mutualism model, we give only half the evidence to the phenomenon E7 and we weaken

the connection to show that the phenomenon is implied weaker by the theory than other phenomena. Computing IMEC with these settings results in an explanatory coherence of 0.779 for the mutualism model and an explanatory coherence of 0.516 for the latent variable model; a change of -0.009 and 0.008, respectively. In other words, the superiority of the mutualism model seems to be robust to the problems with differentiation effects. This example shows how we can incorporate weak predictions as well as weak empirical support when specifying IMEC.

In addition, the latent variable model implies the existence of a biological cause (e.g., Ackerman et al., 2005; Luciano et al., 2005; van der Maas et al., 2006) that constitutes the g-factor (E8). That this predicted phenomenon was never discovered reduces the explanatory coherence of the latent variable theory. Investigating how the discovery of such a biological basis for intelligence would change the explanatory relations of the two theories can tell us whether finding a biological correlate would constitute a critical experiment (e.g., Platt, 1964). In other words, an experiment that could discard the more coherent mutualism theory in favor of the latent variable theory. With IMEC we can test this by modelling a counterfactual world in which a common biological cause of g is discovered. To do so we assign a positive instead of a negative threshold to E8 and compare the theories again. Computing the explanatory coherence assuming a positive threshold on NE8 shows that finding a biological correlate to g would indeed constitute a critical test. After finding such a correlate the explanatory coherence of the mutualism theory would be 0.782, while the latent variable theory increases to 0.836, surpassing even the explanatory coherence of the mutualism theory in the configuration we started with. Thus, the latent variable explanation would be the preferable theory after finding a biological correlate.

The example illustrates how IMEC can compare psychological theories. We showed that the explanatory coherence of two theories can be compared to identify which of them constitutes a better explanation. In addition, by varying thresholds and weights we can account for higher or lower corroboration of phenomena. Finally, modelling counterfactual

states of a theory (e.g., assuming a not yet discovered phenomenon to be discovered) can help us to identify critical experiments that would make a previously inferior explanation the better explanation.

Comparing Creationism and Darwin's Theory of Evolution

One intuitive approach to theory appraisal is selecting the theory that best explains the relevant phenomena.¹⁴ The complement of this intuition is that one should not abandon a theory until there is another theory that is better at explaining or explains more of the relevant phenomena. Thus, a case could be made that the coherence of an explanation should depend on the quality of the available alternative explanations.

One historical case, where a theory lost explanatory coherence because a better alternative explanation became available is when creationism was surpassed by the theory of evolution. As Thagard (1989) points out, Darwin's argument was explicitly comparative. In many places in the *Origin of Species* (Darwin, 1859) he points to facts that the theory of evolution explains while they were unexplainable by the previous idea that species have been created by god. It is also notable that creationism is a very simple theory – the only hypothesis it postulates is the existence of god. Therefore, creationism might seem attractive in light of parsimony. Only a model that considers different epistemic values will be able to refute creationism if a better alternative (evolution) becomes available. In the next section, we first reproduce an example from Thagard (1989)¹⁵ comparing creationism to the theory of evolution. Then we consider whether it was reasonable to believe creationism before the theory of evolution was proposed.

¹⁴ This approach is known in philosophy of science as *Inference to the Best Explanation* (IBE; e.g., Haig, 2009; Harman, 1965; Mackonis, 2013). As far as we know, none of the current attempts at formalizing IBE are without controversy, but there does not appear to be controversy about the intuition or the general principle.

¹⁵ Unlike Thagard (1989) we do not model analogy.

The phenomena and propositions of Darwin's theory as well as creationism are in Tables 2 and 3. The explanatory relations can be found in Figure 9. Comparing the two theories with IMEC indicates that Darwin's theory is the superior explanation (0.820) compared to creationism (0.445).

However, in the case of the theory of evolution, one could argue that not all hypotheses should be considered but only the two core hypotheses of the theory. These are DH2 (Organic beings undergo natural selection) and DH3 (Species of organic beings have evolved). Therefore, we can also calculate the coherence of Darwin's theory as the mean explanatory coherence over only these two hypotheses, instead of all of Darwins hypotheses. If we do so explanatory coherence of evolution increases even further to 0.999. This shows how explanatory coherence changes depending on the set of hypotheses considered elemental for the theory.

Table 2*Evolution vs. Creationism*

Phenomena

E1: The fossil record contains few transitional forms.

E2: Animals have complex organs.

E3: Animals have instincts.

E4: Species when crossed become sterile.

E5: Species become extinct.

E6: Once extinct, species do not reappear.

E7: Forms of life change almost simultaneously around the world.

E8: Extinct species are similar to each other and to living forms.

E9: Barriers separate similar species

E10: Related species are concentrated in the same areas.

E11: Oceanic islands have few inhabitants, often of peculiar species.

E12: Species show systematic affinities.

E13: Different species share similar morphology.

E14: The embryos of different species are similar.

E15: Animals have rudimentary and atrophied organs.

E16: Organic beings in nature undergo variation.

E17: Organic beings increase in population at a high rate.

E18: The sustenance available to organic beings does not increase at a high rate.

Note. Adapted from Thagard (1989).

Table 3*Evolution vs. Creationism*

Darwin's Hypotheses
DH1: Organic beings are in a struggle for existence.
DH2: Organic beings undergo natural selection.
DH3: Species of organic beings have evolved.
DH4: The geological record is very imperfect.
DH5: There are transitional forms of complex organs.
DH6: Mental qualities vary and are inherited.
Creationist Hypotheses
PH1: Species were separately created by God.

Note. Adapted from Thagard (1989).

Figure 9

Explanatory Network of the Comparison Between Creationism and Darwin's Theory of Evolution

Note. Corresponding phenomena and propositions can be found in Tables 2 and 3. Default weight is one but it is split if multiple propositions are needed to explain a phenomenon. The weight on the contradictions is minus four. Thresholds on the phenomena are all two.

However, creationism provided an explanation for the origin of species long before Darwin conceived the theory of evolution. It is interesting to consider whether creationism was a coherent belief system at that time or whether it was always foolish to believe that species have been created by god. To do so, we evaluate the creationist propositions in isolation. In other words, we do not model Darwin's theory and the resulting contradiction. Doing so shows that creationism indeed used to be a remarkably good explanation at the time. Before Darwin's theory emerged as a strong alternative the explanatory coherence of the creationist explanation was in fact 0.999. This high explanatory coherence shows that believing creationism was reasonable before a account for the creation of species was proposed. This example shows not only why people used to believe in creationism but also how a good theory can loose coherence or be refuted once a better theory becomes available.

Discussion

In this paper, we introduced a way to formally assess the quality of theories in psychology by implementing the theory of explanatory coherence using the Ising model. We show that our model smoothly integrates criteria of explanatory breadth, refutation, simplicity, and downplaying of evidence. In addition, by comparing two different models of intelligence, we show that IMEC is capable of comparing more complex theories and helps researchers to think through hypothetical scenarios and to identify critical experiments. Finally, the example comparing the theory of evolution to creationism illustrates that IMEC allows researchers to evaluate how the coherence of a theory changes when a better alternative is proposed. These different possible applications suggest that IMEC is a useful tool to facilitate theory evaluation.

In the above cases, thresholds and weights were set to one since it is usually difficult to establish them objectively from the literature (Thagard, 1989). However, IMEC allows changing those if researchers have empirical reasons to do so. Regarding the evidence for

the phenomena, the thresholds should be scaled according to their strength of empirical support (e.g., Meehl, 1990). It is also important to consider how to scale the edge weights between different propositions and phenomena. The higher the edge weights between propositions and phenomena, the more strongly a theory is supported if there is support for the phenomenon. Based on different approaches for statistical inference, one can think differently about how to specify these edge weights. They could, for example, be scaled according to the probability of the phenomenon absent the theory since the posterior probability of a theory after a confirmed prediction depends upon this parameter (see for example Oberauer & Lewandowsky, 2019). Alternatively, information theory could ground the decision on the edge weights and the thresholds, for example, by trying to establish the distance between predictions and observations based on measures such as the Kullback-Leibler divergence (Kullback & Leibler, 1951).

The process of laying out the compared theories explicitly in terms of their hypotheses, explained phenomena, and the evidence for different phenomena might in itself already aid theory evaluation. First, weaknesses of a theory often become more apparent when formalizing it explicitly and the developed representation of the theory can be discussed with the scientific community. This should help to identify problems and possible modifications of theories already before evaluating them with IMEC. Second, scientists who have not developed a theory which specifies the explained phenomena concretely will notice this when attempting an IMEC implementation and can modify their theory to make more explicit predictions.

Other possibilities for theory evaluation are based on Bayes theorem (Salmon, 2017) or Bayesian networks. While constructing a theory evaluation tool similar to IMEC based on Bayesian networks would certainly be an interesting possibility, it might in practice be difficult for researchers to specify the different prior probabilities and conditional probabilities required. For instance, it will be hard for a scientist to determine the

conditional probability of the inheritance of mental qualities assuming animals do not have instincts.

Finally, IMEC's possible applications reach beyond the area of theory evaluation. Indeed a variety of explanatory processes can be understood in terms of explanatory coherence. Pennington and Hastie (1986) argue that legal decision making can be understood in terms of explanatory coherence and Thagard (1989) evaluates several cases of legal decision making using ECHO. Furthermore, ECHO was used to model psychological processes such as belief revision (Ranney & Thagard, 1988). Therefore, it should in principle be possible to extend IMEC to these areas.

Limitations

As all models, our model has a variety of assumptions and limitations. First, the symmetry of explanatory connections. In practice, theories might be captured more precisely by directed networks as the Bayesian networks described before, although these are more difficult to specify for researchers. Exploring a theory of explanatory coherence based on directed networks would be interesting future research. However, IMEC seems to trade off well between describing the complexity of theories and being simple enough for researchers to specify it in practice.

Second, while the principles of explanatory coherence seem suitable to compare a wide range of cases, they are only hypotheses themselves and, thus, open to revision. In other words, the principles that we based IMEC on may need to be changed again in the future.

Third, a key weakness of using IMEC to compare different theories is that the parameter values need to be specified by the user. Although the default values seem to work well across a wide range of cases; it is sometimes necessary to specify the edges and thresholds manually to incorporate weaker (stronger) evidence or weaker (stronger) predictions. In addition, determining the correct number of assumptions and phenomena is

a difficult task. This process introduces researchers degrees of freedom and might allow a form of “theory-hacking”, where scientists push the explanatory coherence of their own theory. Therefore, when using IMEC to settle theoretical debates in practice it is important to check the robustness of the conclusion by varying the parameter values. While much further research is needed, Thagard (1989) appealed to the following detail maxim, which also applies to IMEC:

In analyzing the propositions and explanatory relations relevant to evaluating competing theories, go into as much detail as is needed to distinguish the explanatory claims of the theories from each other, and be careful to analyze all theories at the same level of detail. Following this maxim removes much of the apparent arbitrariness inherent in trying to adjudicate among theories.

Fourth, in some contexts theory and conceptualization scaffold each other, and it is difficult to construe them independently, or postulate that different theories manifest in identical phenomena (Danziger, 1985, 1993). For example, psychoanalysis and cognitive behavioral therapy might have different concepts of what counts as a valid measurement of depression (i.e., associations or projections versus symptom checklist). However, while this might apply in specific cases, we believe that most phenomena, such as reaction times and error rates or the examples analysed in this paper, can likely be construed independently of theory. In addition, where this limitation applies theory comparison is also intractable with methods other than IMEC.

Fifth, IMEC is capable only of comparing specified theories. The process of generating explanatory hypotheses is not incorporated in IMEC at this point. In other words, finding a theory is still the responsibility of the human theorist. However, several computational algorithms for theory development have been proposed (Romdhane & Ayeb, 2011; Thagard & Nowak, 1988). These algorithms can infer hypotheses from data using certain inference rules. For example, an algorithm called PI (processes of induction) can infer explanatory hypotheses from simple statements (Thagard & Nowak, 1988). For

instance, when instructed that sounds propagate and reflect PI will automatically create the concept of a *sound-wave*. Integrating such an algorithm with IMEC, for example, by evaluating how well the sound-wave theory predicts other observations about sound, could possibly facilitate smooth integration of theory development and theory appraisal.

Future Research

These limitations indicate directions for future research. First, it would be important to establish ways to derive the hypotheses and edge weights more systematically, for example, using text mining approaches to directly extract the explanatory relations from a paper. In addition, researchers could rely on the aforementioned computational algorithms for abduction (e.g., Romdhane & Ayeb, 2011; Thagard, 1988). Finally, severe testing, Bayesian inference and information theory might also guide the choice of edge weights as described before. This line of research could result in general knowledge about the nature of theories that would apply beyond IMEC.

Second, the original ECHO model has a variety of implications beyond the evaluation of scientific theories (Thagard, 1989, 1992). Therefore, it will be interesting to generalize IMEC beyond the realm of theory appraisal in psychology. Thagard (1989) applied his original ECHO model to several cases of legal reasoning, which might also be a promising application for IMEC. In addition, IMEC could also be used to model human reasoning more generally. Ranney and Thagard (1988) show that ECHO could be used to model belief revision in naive physics. Coherence-based models have also been used to model cognition more broadly (Thagard, 2000; Van Rooij, 2008; Van Rooij et al., 2019). It should be possible to apply IMEC to model these kinds of problems with little adaption.

Third, the Ising model shows interesting properties such as phase transitions (Barabási et al., 2016) depending on the value for the entropy parameter β . This parameter describes the heat of the network or the entropy of the model; in other words, if β is zero, the probability of each state is equal, whereas for high values of β , the network

tends to settle in a single state. An interesting property of the Ising model is, that it shows a phase transition for high values of β but not for low ones. A phase transition describes a sudden change between the internal symmetry of the model (Solé, 2011); in the Ising model, this would be a change from an unordered (i.e., some magnets north pole up, others north pole down) to an ordered state (i.e., all nodes north/south up) of the system. Phase transitions have not been used in the present paper and it would be interesting to consider the progression of research lines in terms of phase transitions. One could for example argue, that Popper's idea of falsification describes a phase transition (Popper, 1959), whereas Lakatos (1978) concept of progressive and degenerating research lines describes slower changes. Since the β parameter moderates the occurrence of phase transitions, the Ising model could theoretically incorporate both of these ideas, suggesting a possible unification of different theories in philosophy of science.

Conclusion

Theories are one of the most important tools of cumulative science (Lewin, 1943). Especially in psychology, there has been little progress in the area of formal theory development, despite the high attention that is paid to this topic (Borsboom et al., 2020). One reason for this might be that a systematic, computational approach to evaluating theories lacked in this field. By incorporating a theory of explanatory coherence in the Ising model we developed such an approach. We hope that this will help researchers to evaluate the quality of their theories and will aid in increasing the quality of theories in psychology.

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Appendix

Wegener's Theory of Continental Drift

This example is the most complex theory comparison conducted with IMEC so far. Based on Thagard and Nowak (1988) we analyzed Wegener's theory of continental drift. Wegener (as cited in Thagard and Nowak, 1988) was the first to propose a theory of continental drift based on the observation of strong similarity between the coastlines of Europe and North America. However, his theory was opposed by competing views, mainly the contractionist idea that shrinking of the earth caused earthquakes. The phenomena and propositions of Wegener and his opponents can be found in tables A1 and A2. The explanatory network of this theory comparison is visualized in figure A1. Comparing the two theories with IMEC indicates that Wegener's theory was indeed more explanatory coherence (0.899) compared to contractionist theories (0.534). However, Thagard and Nowak (1988) state that the inference depends on the input. Modelling the argument from papers written by Wegener's opponents makes the contractionist theory more explanatorily coherent. Unfortunately, we cannot reproduce these analyses since they are not available in the paper.

Table A1*Wegener's Theory of Continental Drift*

Phenomena

E1: shape of the Atlantic coastlines match.

E2: There are several North-South mountain chains.

E3: Major folding also occurs along East-West lines.

E4: Tapering North-South blocks curve to the East.

E5: Many species of fossils are represented on both sides of the Atlantic.

E6: The current slow heat loss of the earth requires relatively low temperatures for the ancient crust.

NE6: The earth's crust was significantly hotter in the ancient.

E7: ocean floor is largely level, and continental surfaces are generally 5 km. above it.

E8: Only shallow-sea but no deep-sea fossils are found on land.

E9: Scandinavia appears to be rising with respect to the seafloor.

E10: anomalous gravity measurements have been observed near mountains.

E11: The seafloor and continents are of different composition.

NE11: Large amounts of continental crust can be found under the oceans.

E12: There are no folded mountains on seafloor.

E13: Strata on opposite sides of the Atlantic match.

E14: There are no ancient species in Atlantic, but there are some in Pacific.

E15: Evidence indicates that Scandinavia was tropical and parts of Africa were polar.

E16: Many southern-hemisphere continents have evidence of an ancient polar climate

E17: Measurement of the position of Greenland indicates motion in excess of standard error.

E18: Gravity deficiencies have been measured at oceanic trenches.

E19: Most ancient rocks are greatly folded.

E20: The Atlantic is earthquake-free, but the Pacific has many.

Note. Adapted from Thagard and Nowak (1988).

Table A2

Wegener's Theory of Continental Drift

Wegener's Hypotheses

- W1: The heat content of the earth is rising.
 - W2: The seafloor is depressed around continents by their weight.
 - W3: Crustal blocks swim in magma with only top 5 km showing.
 - W4: resistance of cool oceanic crust to continental movement causes mountain formation.
 - W5: The continents were once all connected.
 - W6: The earth's pole of rotation has moved with respect to the crust.
 - W7: Any large section of the crust is in gravitational equilibrium (Isostasy).
 - W8: Tidal forces pull apart the continents and move them.
 - W9: Polfluchtkraft moves continents toward the equator.
 - W10: Shallow seas may once have been land bridges.
 - W11: Continents move with respect to each other.
-

Wegener's Opponents

- C1: The geographic poles have moved with respect to the crust.
 - C2: The Earth has been contracting since birth due to cooling.
 - C3: The crust is compressed and fractures into blocks.
 - C4: Blocks can override one another.
 - C5: Blocks can subside and become flooded or rise and tip.
 - C6: Land bridges once connected the continents.
 - C7: Isthmus connections served as land bridges.
 - C8: Large sections of the crust are in gravitational equilibrium (Isostasy)
 - C9: The crust swims in a layer of magma.
 - C10: The continents do not move vertically on a large scale.
-

Note. Adapted from Thagard and Nowak (1988).

Figure A1

Explanatory Network of the Comparison Between Wegener's Theory of Continental Drift and his Opponents

Note. Corresponding phenomena and propositions can be found in tables A1 and A2. Default weight is one, but split if multiple propositions are needed to explain a phenomenon. The weight on the contradictions is negative four. Thresholds on the phenomena are all two.

Comparing the Oxygen and the Phlogiston Theory of Combustion

We now compare the phlogiston and the oxygen theory of combustion using IMEC. Thagard (1989) compares both theories and shows that the oxygen theory gives a better account for the process of combustion. However, since IMEC is also capable of evaluating individual theories, we can ask how explanatorily coherent the phlogiston theory was before Lavoisier proposed an alternative explanation based on oxygen. We now first reproduce the example from Thagard (1989) and then evaluate whether it was reasonable to believe the phlogiston theory before the explanation based on oxygen was proposed by evaluating this theory individually.

Up to the 18th century, the most important theory of combustion was the phlogiston theory proposed by Stahl (as cited in Thagard, 1989). This theory implies that combustion occurs due to burned bodies setting free phlogiston. In his essay “*Reflexions sur le Phlogistique*” Lavoisier (as cited in Thagard, 1989) proposed an alternative account of combustion based on oxygen. He claimed that combustion occurs because burned bodies are combining with oxygen in the air. Table A3 shows the phenomena regarding combustion that needed to be explained and the assumptions of Lavoisier’s oxygen theory as well as Stahl’s phlogiston theory. Figure A2 shows the structure of explanations when comparing the two theories.

Table A3*Oxygen and Phlogiston Theory of Combustion*

Phenomena

E1: In combustion, heat and light are given off.

E2: Inflammability is transmittable from one body to another.

E3: Combustion only occurs in the presence of pure air.

E4: Increase in weight of a burned body is exactly equal to weight of air absorbed.

E5: Metals undergo calcination.

E6: In calcination, bodies increase weight.

E7: In calcination, volume of air diminishes.

E8: In reduction, effervescence appears.

Oxygen Hypotheses

OH1: Pure air contains oxygen principle.

OH2: Pure air contains matter of fire and heat.

OH3: In combustion, oxygen from the air combines with the burning body.

OH4: Oxygen has weight.

OH5: In calcination, metals add oxygen to become calxes.

OH6: In reduction, oxygen is given off.

Phlogiston Hypotheses

PH1: Combustible bodies contain phlogiston.

PH2: Combustible bodies contain matter of heat.

PH3: In combustion, phlogiston is given off.

PH4: Phlogiston can pass from one body to another.

PH5: Metals contain phlogiston.

PH6: In calcination, phlogiston is given off

Note. Adapted from Thagard (1989).

Figure A2

Explanatory Network of the Comparison between the Oxygen and the Phlogiston Theory of Combustion

Note. Corresponding phenomena and propositions can be found in table A3. Default weight is one, but split if multiple propositions are needed to explain a phenomenon. The weight on the contradictions is negative four. Thresholds on the phenomena are all two.

Based on this explanatory structure we can now compare the two theories using IMEC. As before the default weight is one, although it is split if multiple propositions are needed to explain a phenomenon. In addition, we modeled strong contradiction with a weight of negative four on the contradictory propositions. Thresholds on the phenomena are all two. Implementing this model in IMEC shows that the oxygen theory's explanatory coherence is 0.790 while the phlogiston theories' explanatory coherence is only 0.543.

In this example, the phlogiston theory is downplayed since it contradicts the better-supported oxygen theory. However, it is interesting to also consider whether the phlogiston theory gave a reasonable account of combustion before Lavoiser developed the oxygen theory. To do this we can investigate the explanatory coherence of the phlogiston

918 theory without modelling oxygen at all. Evaluating the theory in this way we find a higher
919 explanatory coherence of 0.721. This shows that before Lavoisier proposed his theory of
920 combustion, the phlogiston theory was a more appropriate explanation than after he
921 proposed the theory. In other words, this illustrates how old explanations of a set of
922 phenomena lose credibility if better explanations become available.